

GLM Concepts in EMBLEM

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Background

- EMBLEM is a prevalent predictive modeling tool in the insurance industry
- Benjamin Williams from Towers Watson presented a brief intro to EMBLEM on 4/28
- This is a further deep dive to really dig into GLM concepts using EMBLEM screenshots
- Most pictures are direct screenshots from Benjamin William's presentation
- Augmented with other sources
 - 2019 GIS Regulator Advanced Modeling Training
 - Simpler theoretical examples built in Excel to demonstrate concepts
 - References to the CAS GLM monograph



S13,103 observations 244,454 zero weighted | 152 parameters (152 fitted) 0 fixed/aimple aliases 0 complex aliases 568,467 degrees freedom | Polasen Error Log Link Scale (P): 1.00225740682018

Finished iteration: 2

1. Terms in Model

•This is a list of candidate Independent variables

- There are 32 options here
- · These would all have been columns in the input data
- The columns with metrics are not listed here
 - During data input step, you'd specify the target metric fields

•EMBLEM is much more "point and click" than R or Python

- Put a check mark next to the variables you want to include
- Then click "fit"
- R would require typing out the names of the columns
 - Example: Freq_model <- glm(Frequency ~ Age_Youngest + RatingArea + VehicleAge + VehicleValue), family = poisson(link = "log"), data = mydata)

| | T 11.1.1 |
|---|---|
| | l ems in Model |
| | + D Analysis Period |
| | Fandom 10 [Sampling Weights: Modeling] |
| | + D Age of Main Driver |
| | - D Age of Youngest Driver |
| | - dl Simple Factor |
| | + D Age of Youngest Additional Driver |
| | + D Gender of Main Driver |
| _ | + D Gender of Youngest Driver |
| | + C Gender of Youngest Additional Driver |
| | + D Minimum Licence Held |
| | D: Number of Drivers |
| | + D Marikal Status Main Driver |
| | + D NCD Years |
| | + C> NCD Protection |
| | + D Driving Restriction |
| | F D U:e |
| | - C RatingArea |
| | Simple Factor |
| | + D- Voluntary Excess |
| | + D Vehicle Group |
| | + D Make |
| | - D- Vehicle Age |
| | I Simple Factor |
| | - O Vehicle Value |
| | Simple Factor |
| | + D Annual Mieage |
| | D Number of Past Claims |
| | + D- Number of Past Convictions |
| | + C Channel |
| | C> Breakdown Cover |
| | + C> Legal Protection |
| | + D Multi Product Discount |
| | + D Payment Method |
| | + D Payment Frequency |
| | + D Number of Vehicles |
| | + C Credit Score |

1. Terms in Model

•Types of Terms in model

- Potential Rating Variables
 - Variables that you would consider putting in your rating plan
- Control Variables
 - Variables we would not use in rating, but we include so certain effects do not influence our potential rating parameter estimates
 - (CAS GLM Paper Section 5.1.3)
 - Examples are easier to explain
 - Year as a control variable when undeveloped losses are used
 - State as a control variable in a countrywide model because loss level varies by state
- Offset Variables
 - Variables with pre-determined factor that we want our GLM to "work around", not recalculate
 - Limits & Deductibles (CAS GLM Paper Section 9.1)
 - Territory (CAS GLM Paper Section 9.2)

| | Terms in Model |
|-----|--|
| +0 | Analysis Period |
| | Random 10 [Sampling Weight: Modeling] |
| + D | Age of Main Driver |
| EP | Age of Youngest Driver |
| | 🔽 📶 Simple Factor |
| TO | Age of Youngest Additional Driver |
| + D | Gender of Main Driver |
| F-D | Gender of Youngest Driver |
| + D | Gender of Youngest Additional Driver |
| + 0 | Minimum Licence Held |
| + D | Number of Drivers |
| + D | Marital Status Main Driver |
| +-D | NCD Years |
| +-0 | NCD Protection |
| + D | Driving Restriction |
| + 0 | - Use |
| | • RatingArea |
| | 🔽 🖬 Simple Factor |
| + D | Voluntary Excess |
| F D | Vehicle Group |
| + D | Make |
| - P | Vehicle Age |
| 1 | dl Simple Factor |
| - D | Vehicle Value |
| | C gl Simple Factor |
| +D | Annual Mileage |
| + D | Number of Past Claims |
| +D | Number of Past Convictions |
| +D | Channel |
| E D | Breakdown Cover |
| + D | Legal Protection |
| + D | Multi Product Discount |
| + D | Payment Method |
| + D | Payment Frequency |
| +D | Number of Vehicles |
| +0 | Credit Score |
| | |

•Here, Curr Model = Ref Model

- No difference given for "Truncated Description"
- Goodness of Fit statistics are equal
- •This table compares the latest fitted model with a reference model
- •You can save up to 4 reference models
- •Example of a nested model comparison on upcoming slide

| | Current Medel | Reference Hodel | Difference |
|------------------------|--|--|------------|
| Model Label | (none)* | (none)* | |
| Sampling | Modeling | Modeling | |
| Truncated Description | Age of Youngest Driver + RatingOres + | Age of Youngest Driver + RatingArea + | |
| Zero Weighted | 244,484 | 244,484 | 0 |
| Fixed or Simple Alas | 0 | 0 | 0 |
| Complex Alias | 0 | 0 | 0 |
| Fitted Parameters | 152 | 152 | 0 |
| Deviance | 195,816.6 | 195,816.6 | 0 |
| Thi Squared Percentage | | | |
| AICc | 272,088.7 | 272,068.7 | 0 |
| Fitting Result | Cenverged OK | Conversed OK | |

•Here, Curr Model = Ref Model

•No Aliases!

- Simple Alias: 2 columns provide the same info (or extremely correlated)
 - Example:
 - Driver Birth year and Driver Age
 - Married Indicator and Single Indicator
- Complex Alias: 2 or more columns together provide the same info as another column
 - Number of Vehicles and Number of Drivers together explain "Vehicle Driver Ratio"

| | Current Medel | Reference Model | Difference |
|-------------------------|--|--|------------|
| Model Label | (none)* | (none)* | |
| Samping | Modeling | Medeling | |
| Truncated Description | Age of Youngest Driver + RatingArea + | Age of Youngest Driver + RatingArea + | |
| Zero Weighted | 244.484 | 244,484 | 0 |
| Fixed or Simple Alas | 0 | 0 | 0 |
| Complex Alias | 0 | 0 | 0 |
| Fitted Parameters | 152 | 152 | 0 |
| Deviance | 195,816.6 | 195,816.6 | 0 |
| Chil Squared Percentage | | | |
| AlCc | 272,988.7 | 272,068.7 | 0 |
| Fitting Result | Cenverged OK | Conversed OK | |

•Here, Curr Model ≠ Ref Model

- •Difference column tells us many things
 - We added # Drivers
 - We added 4 parameters
 - (n 1) parameters for a categorical field with n levels.
 - We had 1, 2, 3, 4, or 5 drivers, so 4 parameters.

| | Current Nodel | Reference Model | Difference |
|-------------------------|---|--|---------------------|
| Model Label | (none)* | (none)* | |
| Sampling | Modelling | Nodelling | |
| Truncated Description | Age of Youngest Driver + Number of Drivers + | Age of Youngest Driver + RatingArea + | + Number of Drivers |
| Zero Weighted | 264,484 | 244,454 | 0 |
| Fixed or Simple Allas | 0 | 0 | 0 |
| Complex Alias | 0 | 0 | 0 |
| Fitted Parameters | 156 | 152 | 4 |
| Deviance | 195,727.8 | 195,816.6 | -68.8347 |
| Chil Squared Percentage | | Sub-Nodel | 0.0% |
| AICc | 272,044.2 | 272,068.7 | -24.52389 |
| Fitting Result | Converged OK | Converged OK | |

Note: EMBLEM considers all fields "Categorical" until you tell it otherwise!

•Here, Curr Model ≠ Ref Model

- •Difference column tells us many things
 - Deviance went down
 - Always does when adding parameters
 - Chi Squared Percentage is low
 - Implies the larger model is better
 - Chi Squared Percentage is blank if this is not a nested model
 - AICc went down
 - Penalized measure of deviance.
 - Better than deviance to look at

| 12 | Current Nodel | Reference Model | Difference |
|------------------------|---|--|---------------------|
| Model Label | (none) ² | (none)* | |
| Sampling | Modelling | Nodelling | |
| Truncated Description | Age of Youngest Driver + Number of Drivers + | Age of Youngest Driver + RatingArea + | + Number of Drivers |
| Zero Weighted | 244,484 | 244,454 | 0 |
| Fixed or Simple Alias | 0 | 0 | 0 |
| Complex Alias | 0 | 0 | 0 |
| Fitted Parameters | 156 | 152 | 4 |
| Deviance | 195,727.8 | 195,816.6 | -88.8347 |
| Chi Squared Percentage | | Sub-filodel | 0.0% |
| AICc | 272,944.2 | 272,068.7 | -24.52389 |
| Fitting Result | Converged OK | Converged CK | |

Note: BIC is available in EMBLEM but not shown here

3. Volume Summary

•No. Observations is the # rows in input data

•Weight is the sum of the weight metric in our input data

•Weight is the denominator of the target variable

•Target (dependent) variable

- Frequency: Claim Count / Earned Exposures
- Severity: Loss Dollars / Claim Count
- Pure Premium: Loss Dollars / Earned Exposures

| Number of Drivers, | Ne. Observations | Weight |
|--------------------|------------------|---------|
| 1 (1) | 425,299 | 342,035 |
| 2 (2) | 284,855 | 228,790 |
| 3 (3) | 75,607 | 60,466 |
| 4 (4) | 23,431 | 18,666 |
| 5 (5) | 4,010 | 3,127 |

Note: This is likely a frequency model, which means weight is likely earned exposures

3. Volume Summary

• Possible explanation for Weight < No. Observations

- Perhaps each row is one policy year
- Not all policies were insured for the entire policy year
- Therefore the Earned Exposure column is between 0 and 1 for each row
- •Weight does not have to be less than Observations
 - Data could be aggregated up to unique class level
 - Weight should exceed row count in this situation

| Weight | Ne. Observations | Number of Drivers |
|---------|------------------|-------------------|
| 342,035 | 425,299 | 1 (1) |
| 228,790 | 284,855 | 2 (2) |
| 60,466 | 75,807 | 3 (3) |
| 15,665 | 23,431 | 4 (4) |
| 3,127 | 4,010 | 5 (5) |

Note: This is likely a frequency model, which means weight is likely earned exposures

3. Volume Summary

•How the data was aggregated impacts No. Observations

•Consider the following 2 ways to arrange the same claims experience

| | Policy | Gender | Age | Claim | Earned Exposure |
|---|------------------|---------|-----------|-------|-----------------|
| | 1 | М | 16 | 1 | 1 |
| | 2 | F | 16 | 0 | 0.5 |
| | 3 | М | 16 | 0 | 0.25 |
| | 4 | F | 16 | 0 | 1 |
| | 5 | М | 25 | 0 | 1 |
| | 6 | 6 F | | 0 | 1 |
| | 7 | М | 25 | 0 | 1 |
| | 8 | F | 25 | 0 | 1 |
| | 9 | F | 60 | 0 | 0.75 |
| | 10 | F | 60 | 0 | 1 |
| | 11 | F | 60 | 0 | 1 |
| | 12 | F | 60 | 0 | 1 |
| - | | No. Obs | ervations | 12 |] |
| | Earned Exposures | | | 10.5 |] |

Summarized to Rating Class

| Gender | Age | Claim | Earned Exposure |
|--------|-----|-------|-----------------|
| М | 16 | 1 | 1.25 |
| F | 16 | 0 | 1.5 |
| М | 25 | 0 | 2 |
| F | 25 | 0 | 2 |
| F | 60 | 0 | 3.75 |

| No | . Observations | 5 |
|-----|----------------|------|
| Ear | ned Exposures | 10.5 |

4. Graphs by Variable

- Lines you can put on the graph
 - Observed Average
 - Univariate empirical average
 - Fitted Average
 - Univariate average of predictions
 - Parameter Info
 - Model Prediction at Base Levels
 (Point Estimate)
 - Model Prediction at Base Levels -2 SE (Lower Bound)
 - Model Prediction at Base Levels +2
 SE (Upper Bound)



4. Graphs by Variable

- •X Axis
 - Levels of the variable
- Primary Y Axis (Left Side)
 - 4 Target Variable Unit Options
 - Linear Predictor vs. Fitted Value
 - Unscaled vs. Rescaled
 - Examples on upcoming slide
 - "Rescaled Fitted Value" graphs indicated factor
- Secondary Y Axis (Right Side)
 - Weight Volume
 - Useful for identifying where the data is "thin"



4. Graphs by Variable

•Refresher on Linear Predictor with Log Link

| | | | | Predicted Value | Predicted Value Rescaled | Linear Predictor | Linear Predictor Rescaled | |
|----------------------------|--------|--------------|--------|--------------------|--|----------------------|------------------------------|-------------------|
| Frequency at Base Level | 5.0% | β (2.996) | Gender | at Base Levels | at Base Levis <indicated></indicated> | at Base Levels | at Base Levels | Assumption |
| | | | Male | 5.3% | 1.050 | (2.947) | 0.049 | Assume Age 20-30 |
| Gender | Factor | β | Female | 5.0% | 1.000 | (2.996) | - | Assume Age 20-30 |
| Male | 1.050 | 0.049 | | | | | | |
| Female | 1.000 | - | Age |] | | | | |
| A.g.o | Factor | ρ | ≤20 | 10.0% | 2.000 | (2.303) | 0.693 | Assume Gender = F |
| Age | | р 0. сор | 20-30 | 5.0% | 1.000 | (2.996) | - | Assume Gender = F |
| ≤20 aa.aa | 2.000 | 0.693 | 31-60 | 4.0% | 0.800 | (3.219) | (0.223) | Assume Gender = F |
| 20-30 | 1.000 | - | 60+ | 6.0% | 1 200 | (2.813) | 0 182 | Assume Gender – E |
| 31-60 | 0.800 | (0.223) | 00+ | 0.0% | 1.200 | (2.813) | 0.182 | Assume denuer – r |
| 60+ | 1.200 | 0.182 | exp(- | -2.996+.182) = .06 | | -2.996+.182 = -2.813 | | |
| | | | | , | exp(.182) = 1.2 | | β = .182 | |

Note: Fitted Average takes into consideration ALL modeled factors



4. Graphs by Variable

I Model

4. Graphs by Variable





β Pages

- Parameter Number
 - Each non-base level of a categorical variable is a parameter
 - Curve fit continuous variables will have a number based on coefficients in the curve fit
- •Value is fitted β
- •Standard Error helps describe size of confidence interval
 - Standard Error % is SE / abs(Value)
 - Low % green
 - High % red

| A AD Long | WHAT AD LY | analysis East | - Cooklass - I | Ethed Darage | -dearl | | | All the second s | _ |
|---------------------|------------------------------|---------------|-------------------|-----------------------|---------------------------|---------|------------|--|---|
| 6 File | Search Lit View | Madelina | Test 1 | Madeau I | itters j | | | | |
| Con | Streenly Lie Tons | Monend | Toon D | Suppose 1 | Perb | | | anne | |
| ŝ 🖻 | 🖳 🏭 O M 🕕 r | it • 🖪 | BIBF | | | | 🗠 📭 🔟 | 🖾 🧳 Hà | |
| Decimals | - Log B v/c P A | 1 12 | | | | | | | |
| Parameter Number | Name | Value | Standard Error | Standard Error (%) | Alian Indicator (%) | Weight | Weight (%) | Exp(Value) | |
| 49 | Age of Youngest Driver (66) | -0.3232 | 0.06919 | 21.4 | | 6,232 | 1.0 | 0.7238 | |
| 50 | Age of Youngest Driver (67) | -0.2976 | 0.07130 | 24.0 | | 5,635 | 0.9 | 0.7426 | |
| 51 | Age of Youngest Driver (68) | -1.2833 | 0.07266 | 25.6 | | 5,270 | 0.8 | 0.7533 | |
| 52 | Age of Youngest Driver (69) | -0.2310 | 0.07267 | 31.5 | | 5,001 | 0.8 | 0.7937 | |
| 53 | Age of Youngest Driver (70) | -0.1889 | 0.07243 | 38.3 | | 4,859 | 0.7 | 0.8279 | |
| 54 | Age of Youngest Driver (71) | -1.1451 | 0.07196 | 49.8 | | 4,724 | 0.7 | 0.8649 | |
| 55 | Age of Youngest Driver (72) | -0.1788 | 0.07375 | 41.3 | | 4,626 | 0.7 | 0.8364 | |
| 56 | Age of Youngest Driver (73) | -0.1821 | 0.07391 | 40.6 | | 4,604 | 0.7 | 0.8335 | |
| 57 | Age of Youngest Driver (74) | -0.2591 | 0.07367 | 28.4 | | 4,958 | 0.8 | 0.7718 | |
| 55 | Age of Youngest Driver (75) | -0.2263 | 0.07547 | 33.4 | | 4,581 | 0.7 | 0.7975 | |
| 59 | Age of Youngest Driver (76) | -1.1733 | 0.06954 | 40.1 | | 5,224 | 0.8 | 0.8409 | |
| 60 | Age of Youngest Driver (77) | -0.1119 | 0.06758 | 60.4 | | 5,258 | 0.8 | 0.8941 | |
| 61 | Age of Youngest Driver (76) | -0.1322 | 0.06854 | 51.9 | | 5,213 | 0.5 | 0.8762 | |
| 62 | Age of Youngest Driver (79) | -0.1561 | 0.07002 | 44.9 | | 5,077 | 0.8 | 0.8555 | |
| 63 | Age of Youngest Driver (80) | -0.1110 | 0.06879 | 62.0 | | 5,054 | 0.8 | 0.8949 | |
| 64 | Age of Youngest Driver (81) | -0.1590 | 0.07311 | 46.0 | | 4,551 | 0.7 | 0.8530 | |
| 65 | Age of Youngest Driver (82) | -0.0623 | 0.07504 | 120.5 | | 3,897 | 0.6 | 0.9396 | |
| 66 | Age of Youngest Driver (83) | -0.1063 | 0.08243 | 77.5 | | 3,262 | 0.5 | 0.8991 | |
| 87 | Age of Youngest Driver (64) | -0.1883 | 0.19422 | 50.6 | | 2,587 | 0.4 | 0.6301 | |
| 68 | Age of Youngest Driver (85+) | -0.2058 | 0.06313 | 30.7 | | 7,047 | 1.1 | 0.8140 | |
| | Number of Drivers (1) | | | | | 342,035 | 52.4 | | |
| 69 | Number of Drivers (2) | -0.1003 | 0.01255 | 12.5 | | 228,790 | 35.0 | 0.9048 | |
| 78 | Number of Drivers (3) | 0.0203 | 0.01365 | 91.8 | | 60,466 | 9.3 | 1.0205 | |
| 71 | Number of Drivers (4) | 0.0595 | 0.03025 | 50.9 | | 15,606 | 2.9 | 1.0613 | |
| 72 | Number of Drivers (5) | 0.0408 | 0.07145 | 175.2 | | 3,127 | 0.5 | 1.0416 | |
| | Dational see (1) | -0.1235 | 0 12439 | 100.7 | | 1 385 | 0.2 | 0.8839 | |

β Pages

•Alias Indicator (%)

• Higher percent means more likely

Weight

- Denominator of Target
- Weight (%) is the weight in that level

•Exp(Value)

Prediction at base level

| AD Freq | uency - Cil\WithMMAD Fre | | | | | | | |
|--------------------|------------------------------|----------|-------------------|-----------------------|---------------------------|---------|------------|------------|
| Eile | Specify Fit View | Modeling | Took y | Mindow } | Help | | | |
| R I d | | 61 - I B | BIGK | | | | | 17 AL 18 |
| | | | | Par late | | | | |
| ecimals | - Log B v/c P 🛦 | T T | - | | | - | | |
| arameter Number | Name | Value | Standard Error | Standard Error (%) | Aliss Indicator (%) | Weight | Weight (%) | Exp(Value) |
| 49 | Age of Youngest Driver (66) | -0.3232 | 0.06919 | 21.4 | 1.000 | 6,232 | 1.0 | 0.7238 |
| 50 | Age of Youngest Driver (67) | -0.2976 | 0.07130 | 24.0 | | 5,635 | 0.9 | 0.7426 |
| 51 | Age of Youngest Driver (68) | -1.2833 | 0.07266 | 25.6 | | 5,270 | 0.8 | 0.7533 |
| 52 | Age of Youngest Driver (69) | -0.2310 | 0.07267 | 31.5 | | 5,001 | 0.8 | 0.7837 |
| 53 | Age of Youngest Driver (70) | -0.1889 | 0.07243 | 38.3 | | 4,859 | 0.7 | 0.8279 |
| 54 | Age of Youngest Driver (71) | -0.1451 | 0.07196 | 49.6 | | 4,724 | 0.7 | 0.8849 |
| 55 | Age of Youngest Driver (72) | -0.1788 | 0.07375 | 41.3 | | 4,626 | 0.7 | 0.6364 |
| 56 | Age of Youngest Driver (73) | -0.1821 | 0.07391 | 40.6 | | 4,604 | 0.7 | 0.8335 |
| 57 | Age of Youngest Driver (74) | -0.2591 | 0.07567 | 28.4 | | 4,958 | 0.8 | 0.7718 |
| 56 | Age of Youngest Driver (75) | -0.2263 | 0.07547 | 33.4 | | 4,581 | 0.7 | 0.7975 |
| 59 | Age of Youngest Driver (76) | -1.1733 | 0.06954 | 40.1 | | 5,224 | 0.8 | 0.8409 |
| 60 | Age of Youngest Driver (77) | -0.1119 | 0.06758 | 60.4 | | 5,258 | 0.8 | 0.8941 |
| 61 | Age of Youngest Driver (76) | -0.1322 | 0.16854 | 51.9 | | 5,213 | 0.5 | 0.8762 |
| 62 | Age of Youngest Driver (79) | -0.1561 | 0.07002 | 44.9 | | 5,077 | 0.8 | 0.8555 |
| 63 | Age of Youngest Driver (80) | -0.1110 | 0.46879 | 62.0 | | 5,054 | 0.8 | 0.8949 |
| 64 | Age of Youngest Driver (81) | -0.1590 | 0.07311 | 46.0 | | 4,551 | 0.7 | 0.8530 |
| 85 | Age of Youngest Driver (82) | -0.0623 | 0.07504 | 120.5 | | 3,697 | 0.6 | 0.9396 |
| 66 | Age of Youngest Driver (83) | -0.1063 | 0.08243 | 77.5 | | 3,262 | 0.5 | 0.8991 |
| 87 | Age of Youngest Driver (64) | -0.1863 | 0.19422 | 50.6 | | 2,587 | 0.4 | 0.6301 |
| 68 | Age of Youngest Driver (85+) | -0.2058 | 0.06313 | 30.7 | | 7,947 | 1.1 | 0.8140 |
| - | Number of Drivers (1) | | | | | 342,035 | 52.4 | |
| 69 | Number of Drivers (2) | -0.1003 | 0.01255 | 12.5 | | 228,790 | 35.0 | 0.9046 |
| 78 | Number of Drivers (3) | 0.0203 | 0.01865 | 91.8 | | 60,466 | 9.3 | 1.0205 |
| 71 | Number of Drivers (4) | 0.0595 | 0.03025 | 50.9 | | 16,606 | 2.9 | 1.0613 |
| 72 | Number of Drivers (5) | 0.0408 | 0.07145 | 175.2 | | 3,127 | 0.5 | 1.0416 |
| 73 | RatingArea (1) | -0.1235 | 0.12439 | 100.7 | | 1,385 | 0.2 | 0.8839 |
| | | - | | | | | | |

β Exporter

Same options as graph options

- Linear Predictor vs. Fitted Value
- Unscaled vs. Rescaled
- Exports comprehensive indicated list to Excel
 - Base appears at the top (intercept term)
 - Simple factors appear below the base
 - Interaction factors appear below the simple factors

Example is "Rescaled fitted value"

Every base level shows 1.000

| 4 | A | Ð | C | 0 | E | F | G | H | 1 | 1 | K | 1 | M | N |
|---|-----------|--------------|---------|----------------|-------------|---|------------|--------|---|-----------|--------|---|------------|-------------|
| 8 | | - | 0.0530 | | _ | | | | | | | | | |
| 4 | 15869 | | 0.05.87 | | _ | | | - | | - | | | _ | |
| | | | _ | - | | | | - | | | | | | |
| | Ane of) | (oundest l | Driver | Numbe | r of Driver | | atina Ar | 0.0 | | Vehicle | 0.ne | | Vehicle V | /alue |
| | - Be AL | Verigeet | on the | The section of | | | enen igrei | | | A A INCOM | - Be | | TOTICIO V | - Million W |
| | Age of Yo | unnest Drive | or | Number | of Drivers | R | ationAsos | | | Vehicle A | ae | | Vehicle Va | line |
| | 18 | 0.0008 | | 4 | 1,0000 | - | | 0.8839 | | Ð | 1,4190 | | >=0 <1000 | 1,149 |
| | 19 | 1,7317 | | 2 | 6,50461 | 2 | | 0.9584 | | 1 | 1,4781 | | >=1000 < | 1.076 |
| 0 | 20 | 1.9453 | | 3 | 1.0205 | 3 | | 0.8908 | | 2 | 1.4743 | | >=2000 <3 | 0.727 |
| 1 | 21 | 1.4713 | | 2 | 1.0613 | 2 | | 0.9265 | | 3 | 1.3032 | | >=3000 <4 | 0.790 |
| 2 | 22 | 1.3777 | | 5 | 1.0415 | 5 | | 1.0199 | | 2 | 1.2956 | | >=4000 << | 0.835 |
| 5 | 23 | 1.0859 | | | 10012000 | 8 | | 1.0128 | | 5 | 1.2070 | | >=5000 <8 | 0.925 |
| 1 | 24 | 1.1101 | | | | 7 | | 0.9768 | | 8 | 1.1377 | | >=6000 <7 | 1.001 |
| 5 | 26 | 1.2526 | | | | 3 | | 1,0000 | | 7 | 1.0701 | | >=7000 <8 | 1.023 |
| 8 | 26 | 1.1557 | | | | 3 | | 1,1033 | | 3 | 1.0177 | | >=8000 << | 1.011 |
| 7 | 27 | 1.1948 | | | | 1 | 0 | 1.0932 | | 5 | 1.0000 | | >=9000 <1 | 1.074 |
| 8 | 28 | 1,1194 | | | | 5 | 1 | 1.0871 | | 510 | 0.9069 | | >=10000 < | 1.117 |
| 9 | 29 | 1.0401 | | | | 1 | 2 | 1.1448 | | 511 | 0.9428 | | >=11000 < | 1,112 |
| 0 | 30 | 1.0951 | | | | 1 | 3 | 1.1329 | | 12 | 0.8982 | | >=12000 < | 1.086 |
| 1 | 31 | 1.0850 | | | | 0 | 4 | 1.0908 | | 13 | 0.9970 | | >=13000 < | 1.14 |
| 2 | 32 | 0.9776 | | | | 0 | 5 | 1,1997 | | 14 | 0.7489 | | >=14000 < | 1.138 |
| 3 | 33 | 0.9843 | | | | 9 | 6 | 1.2730 | | 715 | 0.6676 | | >=15000 < | 1.177 |
| 1 | 34 | 1.0176 | | | | 9 | 7 | 1,1963 | | 96 | 0.7506 | | >=16000 < | 1.19 |
| 5 | 36 | 1.0101 | | | | | 8 | 1.1608 | | 17 | 0.6718 | | >=17000 < | 1, 183 |
| 5 | 36 | 1.0000 | | | | 3 | 9 | 0.9291 | | 18 | 0.6154 | | >=18000 < | 1.21 |
| 1 | 37 | 0.9325 | | | | 2 | 0 | 1.1090 | | 99 | 0.7174 | | >=19000 < | 1.26 |
| | 38 | 1.0268 | | | | U | nknown | 1.0000 | | 20 | 0.7042 | | >=20000 < | 1.201 |
| 9 | 39 | 0.9399 | | | | | | | | 21 | 0.6910 | | >=21000 < | 1.184 |
| 2 | 40 | 0.9336 | | _ | - | | | | | 22 | 0.7864 | | >=22000 < | 1.26 |
| 1 | 41 | 0.9578 | | | | | | | | 23 | 0.6326 | | >=23000 < | 1.34 |
| 2 | 42 | 0.9813 | | | | | | | | 24 | 0.7939 | | >=24000 < | 1.438 |
| 3 | 4.3 | 0.9305 | | | | | | | | 25 | 0.8879 | | >=25000 + | 1,44 |
| 1 | 44 | 0.9492 | | | | | | | | 26 | 0.6482 | | >=26000 4 | 1.31 |
| 5 | 45 | 0.9233 | | | | | | | | 27 | 0.7585 | | >=27000 < | 1.51 |
| | 46 | 0.9281 | | | | | | | | 28 | 0.4052 | | >=29000 < | 1.45 |
| 1 | 41 | 0.9500 | | | | | | | | 29 | 0.6971 | | >=29000 < | 1.69 |
| 5 | 48 5 4 | 0.8264 | | | | | | | | 30+ | 0.3424 | | >=30000 < | 1.41 |
| | 49 | 0.8865 | | | _ | | | | | | 10.000 | _ | >=31000 < | 1.72 |
| | 90 8. | 0.9226 | | | | _ | | | | | | | 3#32000 4 | 1.36 |
| 1 | 51 | 0,8889 | | | | | | | | _ | | | >=33000 < | 1.81 |
| 4 | 52 | 0.8237 | | | | | | | | | | | >=34000 < | 1.64 |
| 5 | 53 | 0.8165 | | | | | | | | | | | >=35000 | 1.99 |

Curve Fitting (Before)

- Every level of Vehicle Age was it's own parameter
 - Essentially treated like a categorical variable
- Obvious pattern emerges on the left side
- Confidence interval expands on the right side
 - Caused by low data volume
 - Confidence intervals impacted by choice of base level
 - CAS GLM Paper Section 2.4.3
- "Rescaled Predicted Value" is essentially the indicated factor
 - Base = 1.000



Curve Fitting (After)

Number of parameters greatly reduced

of degrees in polynomial fit

Factors now reflect a smooth pattern

- Note, factors may appear slightly curved even on a 1 degree fit
 - The graph on the right is a 1 degree fit
 - Still appears slightly curved
 - This is because of the log link function
- Large continuous variables should be logged before fitting a curve
 - CAS GLM Paper (Section 2.4.1)



Curve Fitting (Before and After)

 You can compare fitted model to reference model at any time

Reference Model

- Blue Triangles
- Before Curve Fitting
 - Lots of parameters
 - Not smooth at all

Fitted Model

- Green Circles
- After Curve Fitting
 - Few parameters
 - Monotonic if desired
 - Smooth factors limit disruption



Correlation Tests

Determine an acceptable cutoff

Towers Watson Emblem

| Factor (#Levels) | CalYear (12) | DurYear (18) | Gender (2) | ncurredAge (56) | IssueAge (46) | arital_Status (2) | ^ |
|---------------------------|--------------|--------------|------------|-----------------|---------------|-------------------|---|
| CalYear (12) | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| DurYear (18) | 0.190 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| Gender (2) | 0.005 | 0.005 | 0.000 | 0.000 | 0.000 | 0.000 | |
| IncurredAge (56) | 0.049 | 0.155 | 0.060 | 0.000 | 0.000 | 0.000 | |
| (ssueAge (46) | 0.036 | 0.043 | 0.084 | 0.320 | 0.000 | 0.000 | |
| Marital_Status (2) | 0.017 | 0.036 | -0.190 | 0.144 | 0.193 | 0.000 | |
| StateAbbr (51) | 0.041 | 0.048 | 0.022 | 0.029 | 0.030 | 0.079 | |
| TQ_Status (3) | 0.068 | 0.089 | 0.023 | 0.085 | 0.068 | 0.047 | |
| Cov_Type (3) | 0.072 | 0.197 | 0.030 | 0.227 | 0.203 | 0.087 | |
| Infl_Rider_Description (4 | 0.062 | 0.074 | 0.032 | 0.157 | 0.193 | 0.124 | |
| Region (4) | 0.052 | 0.076 | 0.013 | 0.061 | 0.042 | 0.050 | |
| EliminationPeriod (5) | 0.050 | 0.061 | 0.019 | 0.045 | 0.037 | 0.053 | |
| BenefitDollars (10) | 0.065 | 0.092 | 0.031 | 0.126 | 0.105 | 0.052 | |
| | 0.045 | A 655 | A 845 | 0.105 | | > | |



•Visualization shows thicker lines for stronger correlations

•Correlation Statistics appear in a table that can be easily exported

Multi-way Graphs Checking for Interactions

Multi-way test: Gender vs. Vehicle Age

Colors

- Blue for male, Green for female
- Volume split nearly 50/50
- Looking at the graph WITHOUT interaction fitted in the model
 - Actual vs Expected for "Male" looks good
 - Actual vs Expected for "Female" looks good
- If our model fits both groups well without the interaction, it's superfluous
- Chi-Square test comparing a model with the interaction and a model without doesn't pass significance.



Multi-way Graphs Checking for Interactions

- Multi-way test: Gender vs. Driver Age
- Colors
 - Blue for male, Green for male
 - Volume split nearly 50/50
- Looking at the graph WITHOUT interaction fitted in the model
 - Actual vs Expected biased low for young males
- Our model fails without an interaction
- Chi-Square test comparing a model with the interaction and a model without DOES pass significance test.



Other EMBLEM tools

Backwards and Forwards Stepwise Regression Tests

- Running a backwards stepwise regression on a final model highlights potentially insignificant terms
- Automated Interaction Tests
- Set Offset Factors
 - Coverage options (limits/deductibles) and territory are often better handled outside GLM
 - CAS GLM Paper (Sections 9.1 & 9.2)
- Convert model to a scoring model

Reference

•CAS GLM Paper

• <u>https://www.casact.org/pubs/monographs/papers/05-Goldburd-Khare-Tevet.pdf</u>