



# *Tree-based models*

*NAIC June 29<sup>th</sup>, 2021*

Caolan Kovach-Orr, Ph.D., CSPA  
Vahid Meimand, Ph.D.



# Caolan Kovach-Orr, PhD, CSPA

## Senior Data Science Manager: Data Engineering & New Technologies

### BACKGROUND

Caolan Kovach-Orr leads the DENT team for ISO Insurance Analytics, Verisk Analytics. He is a Ph.D. data scientist with 12+ years of experience in big data, analytics, machine learning, and new product development. Caolan combines deep subject matter expertise, technical leadership, and a passion for engineering novel solutions to difficult problems.

Before joining Verisk, Dr. Kovach-Orr was a research data scientist who leveraged high performance cluster computing to investigate and understand how variation affects the risk of collapse for ecosystems threatened by environmental change.

### PROFESSIONAL DESIGNATIONS AND ACTIVITIES

Caolan is a CAS Certified Specialist in Predictive Analytics. He takes an active role in presenting at conferences and educating industry professionals (actuaries, regulators, data scientists) on advances in data science, machine learning, and insurance modeling.

### EDUCATION

- Postdoctoral Researcher, McGill University, Canada
- PhD in Theoretical Biology, McGill University, Canada
- BSc in Ecology & Evolutionary Biology, Rutgers University, New Brunswick, NJ
- Minor in Geographic Information Systems, Rutgers University, New Brunswick, NJ

### SELECTED PROJECTS

#### Risk Analyzer Commercial Auto Liability Symbols (RACA)

Developed a methodology to interpret Machine Learning Algorithms, which allowed Verisk to attain regulatory approval for the US's first Machine Learning Ratemaking product based on traditional variables (e.g., horsepower, airbags, etc.)

#### AWS Insurance Analytics Environment

Engineered CPU, GPU, and Hadoop environments for use by the Insurance Analytics teams. These environments are capable of providing a 1000-5000x speed up over SAS Grid while simultaneously reducing costs by 2+ orders of magnitude (>100x cheaper)

#### Voice of the Customer (NLP)

Enhancing the value of Verisk customer feedback by using advanced data engineering techniques, Natural Language Processing, and dashboard reporting

#### Ethical AI/ML

Leading efforts to identify and remove bias from data so that Protected Classes are not unfairly impacted by Verisk products

### INTERESTS AND EXPERTISE

- Data Science | Machine Learning | Analytics
- Data Engineering | Architecture
- Rating Models | Underwriting | Internal Projects
- Big Data Architecture & Solutions
- Accelerated Computing (GPU & FPGA)
- Optimization | Design
- Complex Systems | Systems Modeling
- Solution Engineering
- Insurance: Personal and Commercial
- Academia | Consulting
- Grant and proposal writing



## Vahid Meimand, PhD

### Senior Lead Data Scientist

#### BACKGROUND

Vahid Meimand leads a data science team at ISO insurance analytics where he uses data and analytics to build products in the insurance underwriting domain. He received his Ph.D. in engineering at John Hopkins University. Vahid has significant experience in applying advanced statistical learning theory, machine learning algorithms, and visualization techniques to drive insight from data in insurance, infrastructure, energy, and health sectors. Prior to Verisk, Vahid was Lecturer at Purdue University in the school of mechanical engineering. He also performed consulting work at NBM Technology as a Senior/then Principal Engineer for 5 years. There, he led projects on surveying railroad tracks and inspecting bridges using computer vision and machine learning algorithms.

#### PROFESSIONAL DESIGNATIONS AND ACTIVITIES

- Johns Hopkins Data Science Specialization Certificate
- Currently pursuing CSPA and ACAS credentials

#### EDUCATION

- PhD in Civil Engineering, John Hopkins University
- MS in Civil Engineering, Johns Hopkins University and University of Tehran
- BS, Civil Engineering, University of Tehran

#### SELECTED PROJECTS

##### Hazard Detection Computer Vision

Hazard detection is a product to facilitate underwriting process by allowing insurer's customers do self inspect their properties. It uses imagery data from personal properties as the input and determines if any risk/hazard from a set list exist in the given property. Deep learning convolution neural networks are trained on a huge set images collected from properties across the US.

##### Roof Age Model

Roof Age product include the roof age and an assigned confidence score for about 80 million residential home across the US. A predictive model is built to estimate the roof age for 75% of the homes for which the roof age is not know through different sources.

##### Connected Homes Model-Ready Data

Working with the IoT team to extract and transfer smart homes data. The data is provided by Vivant (a home security company) and is transferred to various insurance carriers. Tasks include receiving, cleansing, filtering, and matching large amount of data from both sides.

##### BOP Rating Factors

Updating the rating factors for the Business Owner Policies using transactional data provided by insurers. Also updating the grouping of the different classes of businesses. GLM is the main modeling technique used.

#### INTERESTS AND EXPERTISE

- Data Science | Analytics | Machine Learning
- Supervised and unsupervised predictive analytics
- Deep learning and Computer Vision
- Statistics
- Big data

# Agenda

- Introduction & Background
- CART: Simple Trees
- Beyond CART: Bagging & Boosting
  - AKA Random Forest & Gradient Boosting
- Interpretation
- Evaluation of Tree based models

# Traditional Insurance Ratemaking

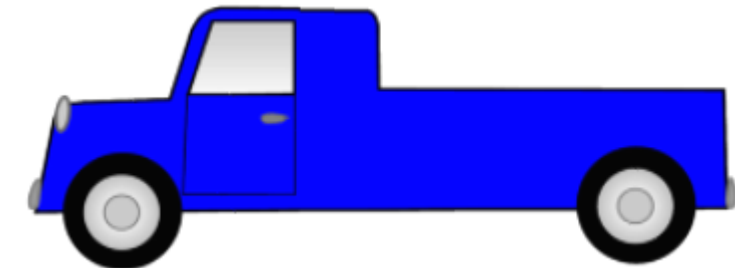
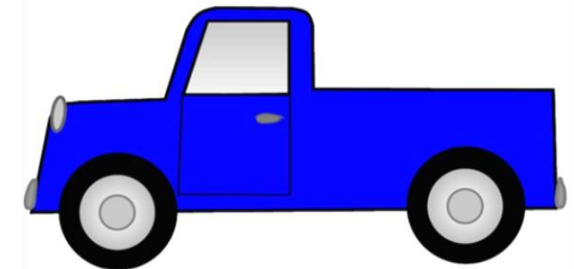
## Generalized Linear Models

- Relate Multiple Predictors to Frequency, Severity, or Pure Premium
- Not Necessarily “Linear”
- Well established for Ratemaking & Underwriting
- Proven Track Record

	Linear Models
	GLM
Interpretability	Green
Likelihood of Overfitting	Grey
Sensativity to Collinearity	Red
Relative Predictive Power Given Strong Signal	Green
Relative Predictive Power Given Weak Signal	Grey
Relative Predictive Power Given Complex Variable Behaviors (Interactions + Mixtures + Non-linear Effects)	Red
Skill Required	Red
Speed of Development	Red



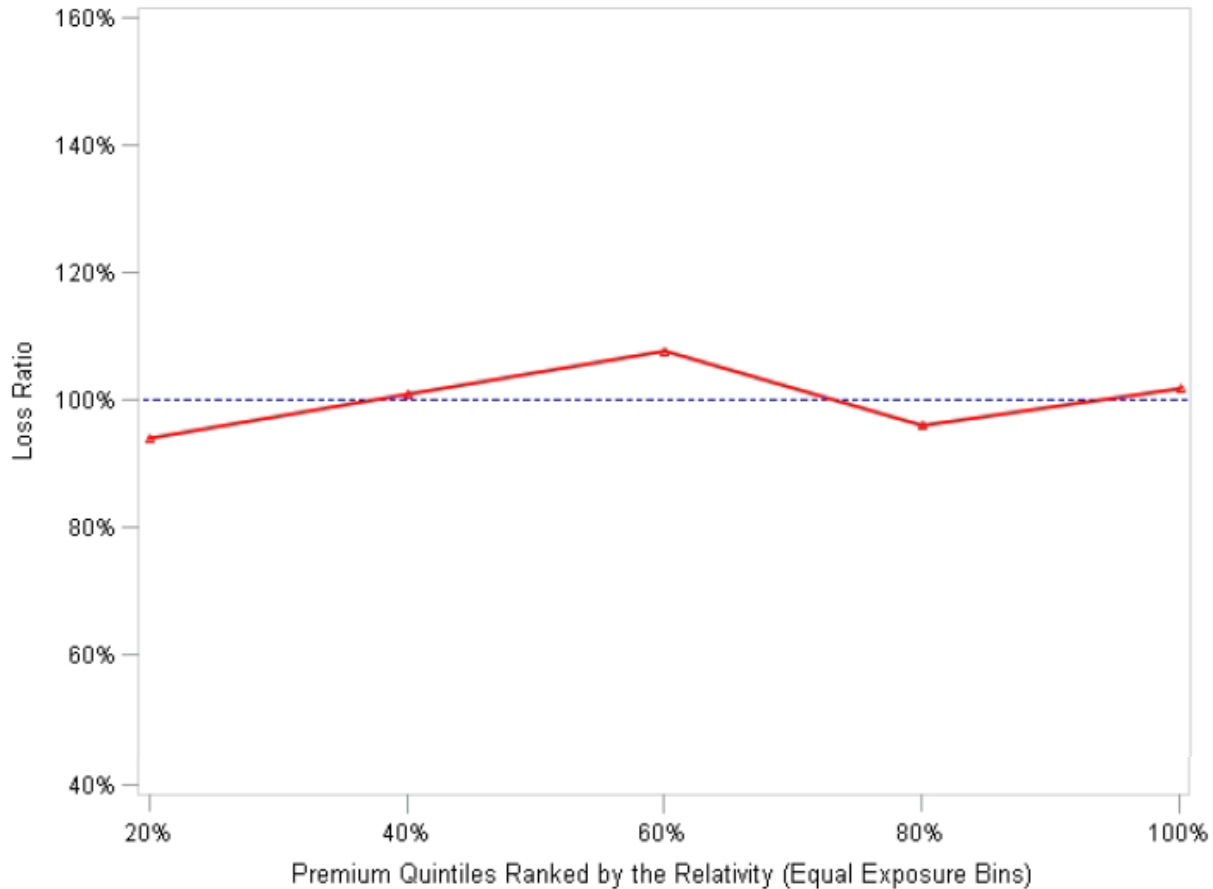
**Segmentation, Body Style, Vehicle Weight, Wheelbase, Engine Size, MSRP, Fuel Type, etc.**





# GLMs and GBTs applied to Comm Auto Liability

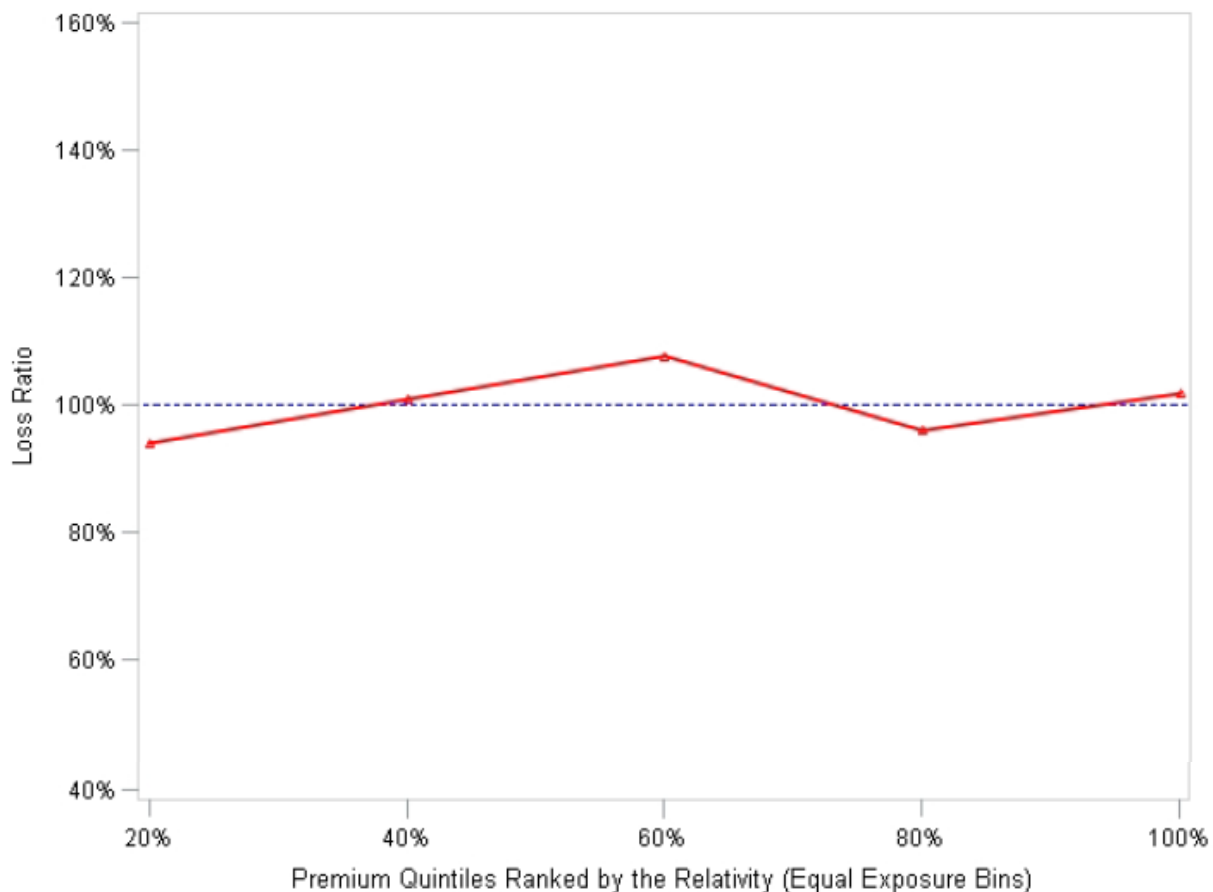
CA GLM (on test data)



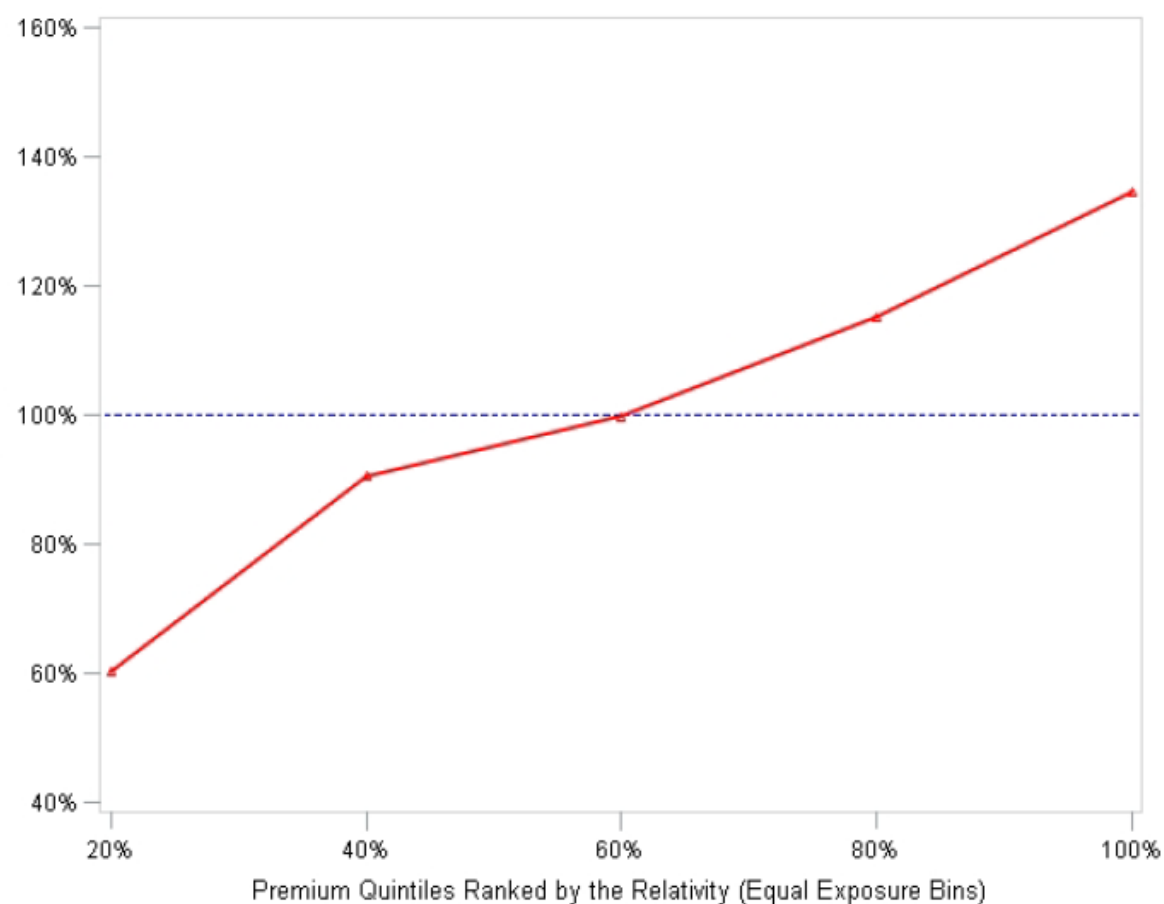


# GLMs and GBTs applied to Comm Auto Liability

## CA GLM (on test data)




## CA GBT Symbols (on test data)





# Level Setting

- Not artificial intelligence- we build a model
  - Doesn't adapt, change, evolve, etc.
  - Supervised
- Exactly the same as
- We can only
- This isn't a model
  - First
  - First
  - Use
  - First
  - Use



DEGREE PROJECT IN MATHEMATICS,  
SECOND CYCLE, 30 CREDITS  
STOCKHOLM, SWEDEN 2018

**Claims Reserving using  
Boosting and Generalized  
Models**

MARCUS AHLGREN

**DELTA BOOSTING: A BOOSTING APPLICATION IN  
ACTUARIAL SCIENCE**

Simon CK Lee<sup>1</sup> and Sheldon Lin<sup>2</sup> and Kristin Aasland<sup>1,3</sup>

<sup>1</sup> KU Leuven, Belgium  
<sup>2</sup> University of Toronto  
<sup>3</sup> University of Amsterdam,  
May 1, 2015

Balancing robust statistical  
Gradient



**Expert Systems with Applications**  
Volume 39, Issue 3, 15 February 2012, Pages 3659-3667

**Gradient boosting trees for auto insurance loss cost  
modeling and prediction**

Leo Guelman  

**Insurance Premium Prediction via Gradient  
Tree-Boosted Tweedie Compound Poisson  
Models**


YI YANG\*, WEI QIAN† AND HUI ZOU‡

April 22, 2016

Leo Guelman, Simon Lee, and Helen Gao

Royal Bank of Canada - RBC Insurance

March, 2012



Jct  
model



# CART: Classification And Regression Trees

- Non-parametric method for Classification And Regression
- Segments the predictor space into simple regions (terminal nodes) following a set of splitting rules

- **Pop:** 2,500,000

- **Pop:** 350,000
- **Par:** Segmentation Code
- **Threshold:** Compact Van vs. All Others
- **Left:** 50,000
- **Right:** 300,000

Power  
150 vs.  $\geq 150$

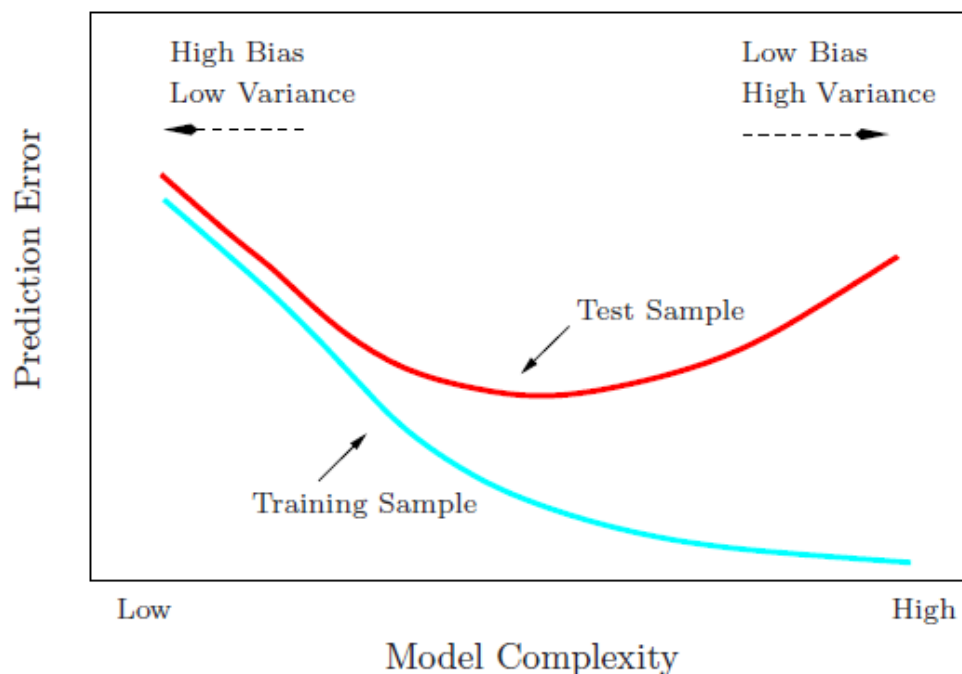
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	Linear Models
	GLM
Interpretability	Green
Likelihood of Overfitting	Grey
Sensativity to Collinearity	Red
Relative Predictive Power Given Strong Signal	Green
Relative Predictive Power Given Weak Signal	Grey
Relative Predictive Power Given Complex Variable Behaviors (Interactions + Mixtures + Non-linear Effects)	Red
Skill Required	Red
Speed of Development	Red

# Bias-Variance trade-off

$f = ?$

$$Y = f(X) + \epsilon$$



Source: Elements of Statistical Learning II

$$EPE = E\{Y - \hat{f}(x)\}^2$$

$$= E\{Y - f(x)\}^2 \quad \text{(Irreducible Error)}$$

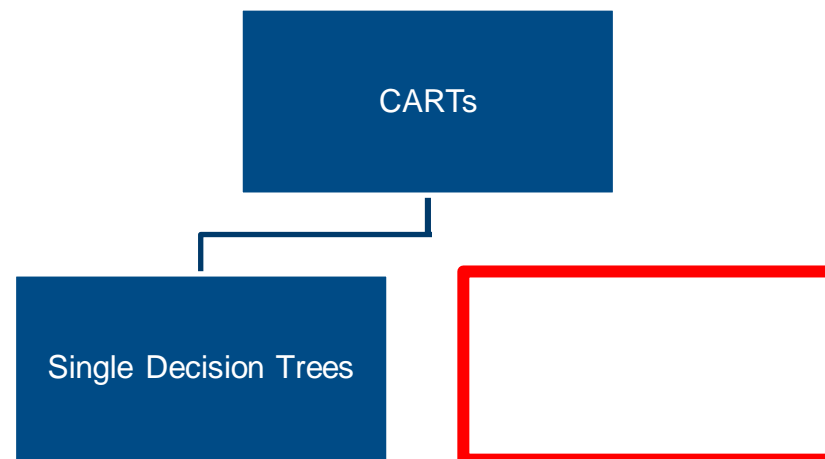
$$+ \{E(\hat{f}(x)) - f(x)\}^2 \quad \text{(Bias)}$$

$$+ E\{\hat{f}(x) - E(\hat{f}(x))\}^2 \quad \text{(Variance)}$$

# Beyond CART: Overcoming the limitations of the Single Decision Tree

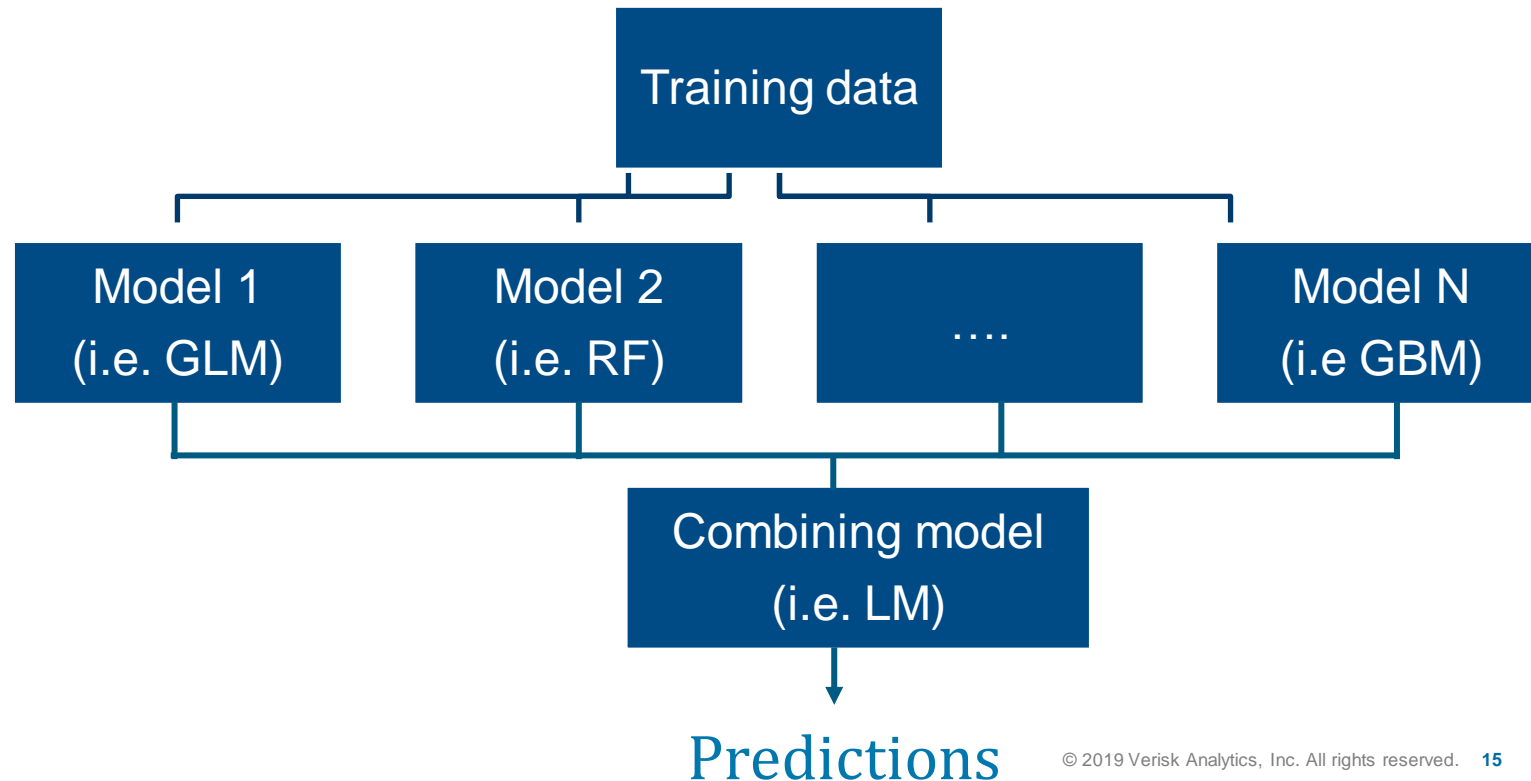
## Single decision tree:

- Low bias, high variance
- Predictive power is not great



# Ensemble Learning

- **Ensemble learning can be broken down into two tasks:**
  - Developing a population of base learners from the training data
  - Combining them to form the composite predictor.
- **Bagging and Boosting are two examples of ensemble learning**



# Ensemble Learning

## Advantages

Improved accuracy

Improved robustness and stability

Works for linear and simple as well as non-linear and complex relationships in the data.

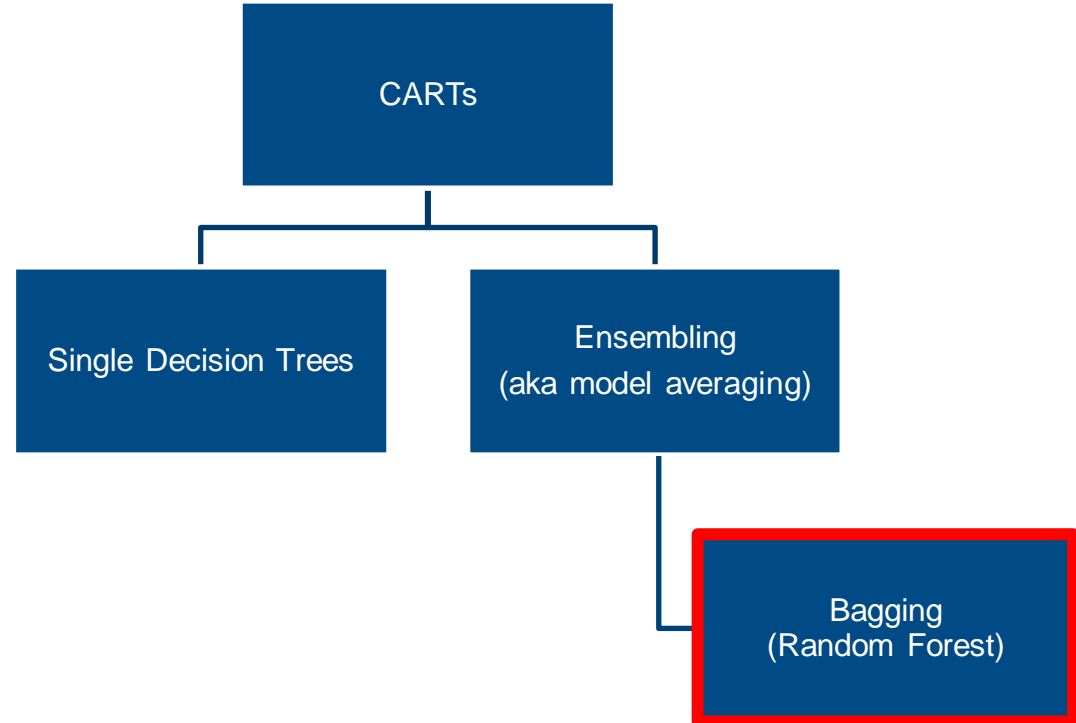
## Disadvantages

Reduced model interpretability

Time-consuming

Model selection for creating an ensemble is often a difficult task.

# Beyond CART: Overcoming the limitations of the Single Decision Tree



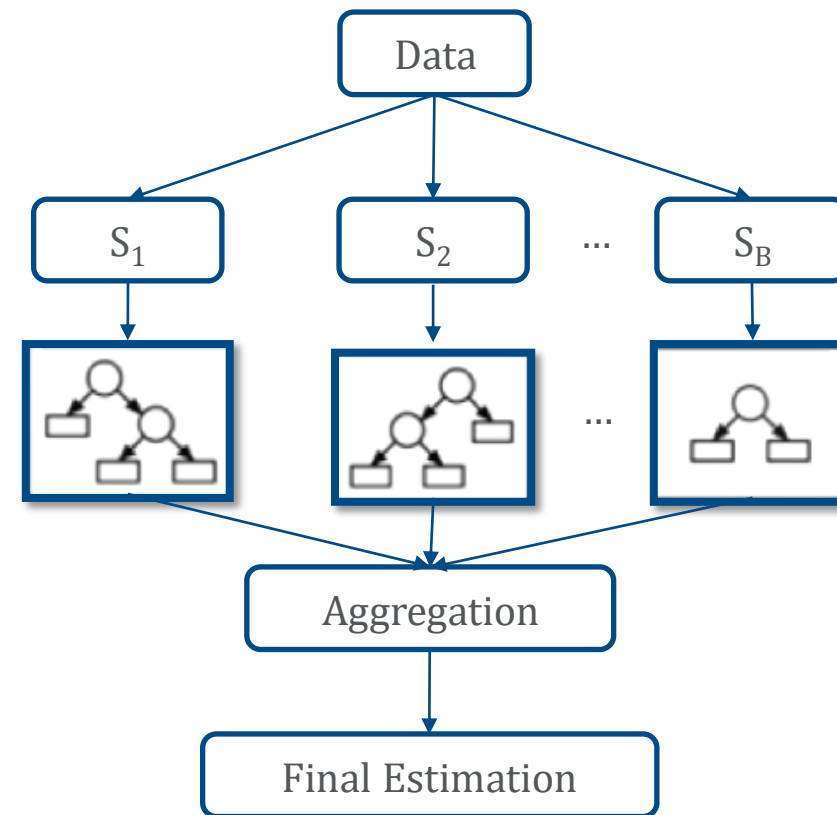
# Bagging (Random Forest)

# Bagging

- Bagging (bootstrap aggregating) averages prediction over a collection of bootstrap samples, thereby reducing its variance.
- B models are created using B bootstrap samples of the data, Then bagging estimate is denoted by:

$$\hat{f}_{bag}^B = \begin{cases} \frac{1}{B} \sum_{b=1}^B T_b(x) & \text{regression} \\ \text{Majority Vote} & \text{classification} \end{cases}$$

Bagging was introduced by: Leo Breiman, 1994.







## Why Bagging is such a great idea?

A decision tree is a very low bias but high variance model

We need to reduce the variance, how?

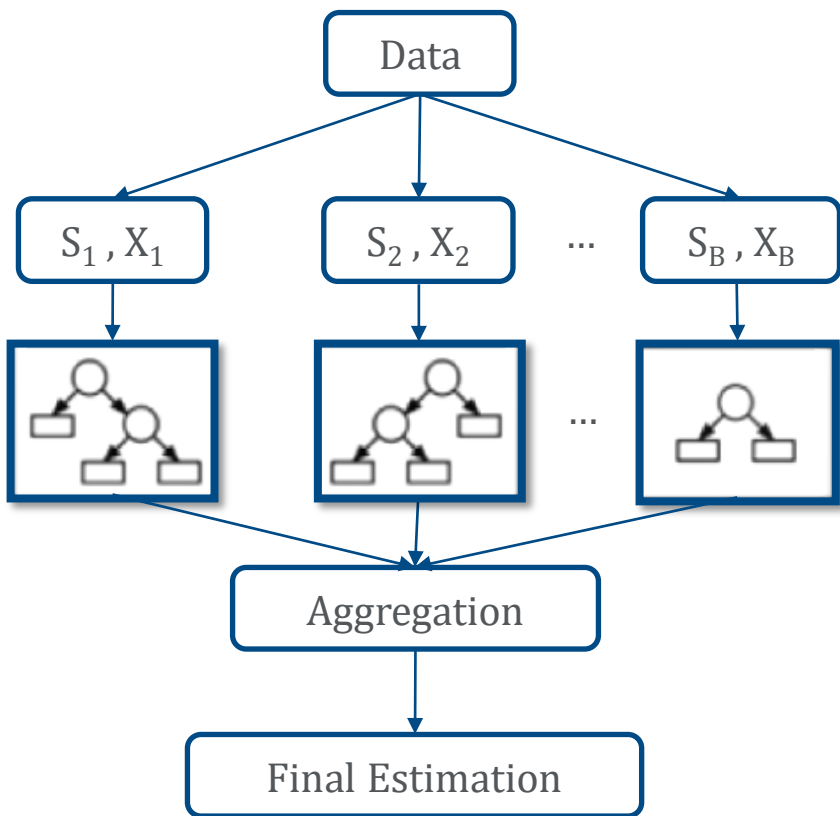
- Simple idea: aggregate many trees which is still a low bias model

If the trees are completely uncorrelated, variance is divided by the number of trees

If the trees are fully correlated, we gain nothing

Usually, we are somewhere in between

# Bagging to random forest



$S_1$  to  $S_B$ : B bootstrap samples from data  
 $X_1, X_B$ : B random subsamples of the predictors to decrease the correlation between the trees

$$\hat{f}_{rf}^B = \begin{cases} \frac{1}{B} \sum_{b=1}^B T_b(x) & \text{regression} \\ \text{Majority Vote} & \text{classification} \end{cases}$$

$$Var_{rf} = \rho \sigma^2 + \frac{1 - \rho}{B} \sigma^2$$

Tuning Parameters:

- Fraction of the predictors to randomly select for each tree
- Minimum terminal node size
- Number of trees – mainly for computational efficiency, rarely cause overfitting
- Depth of trees

Random Forest was introduced by: Leo Breiman, 2001.



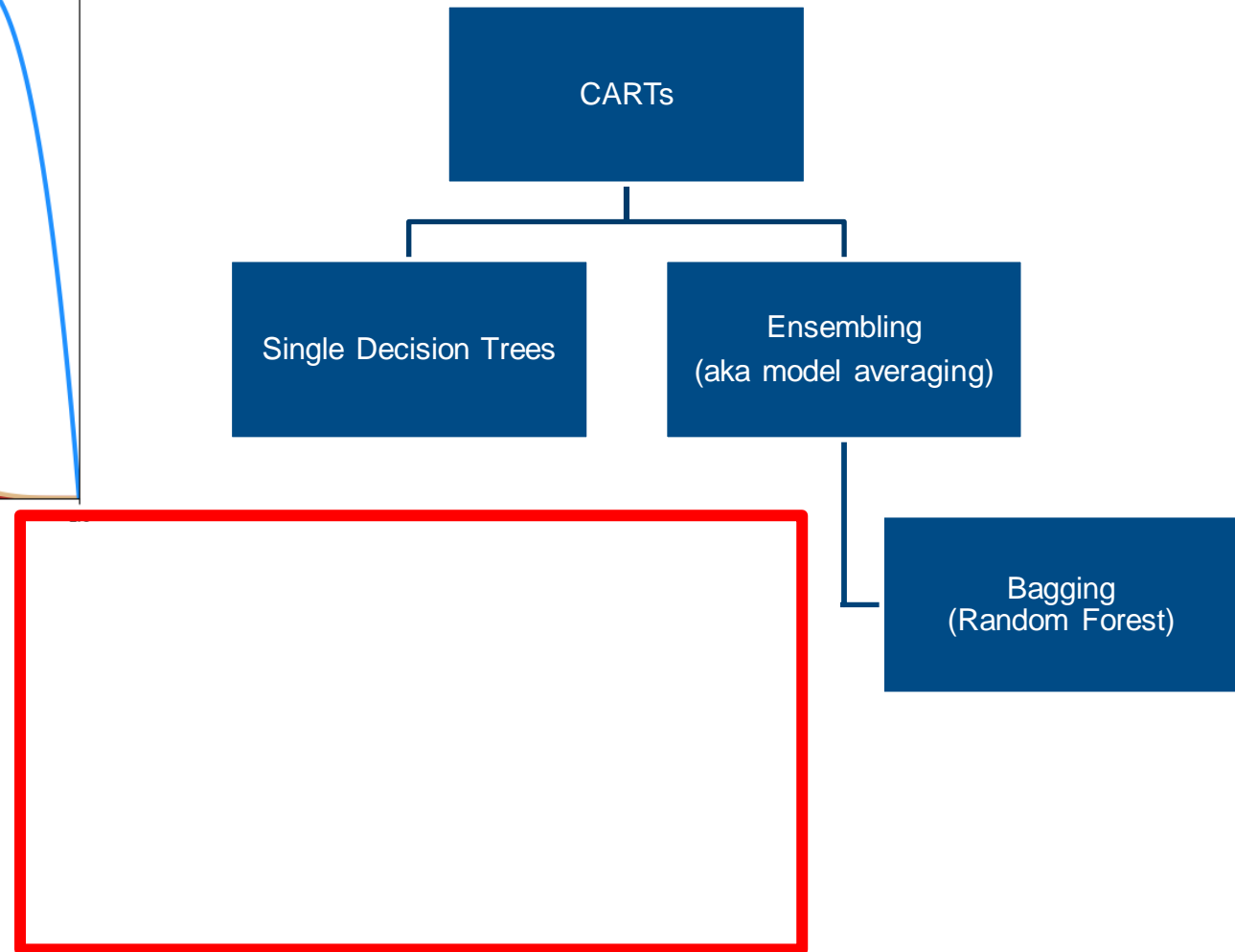
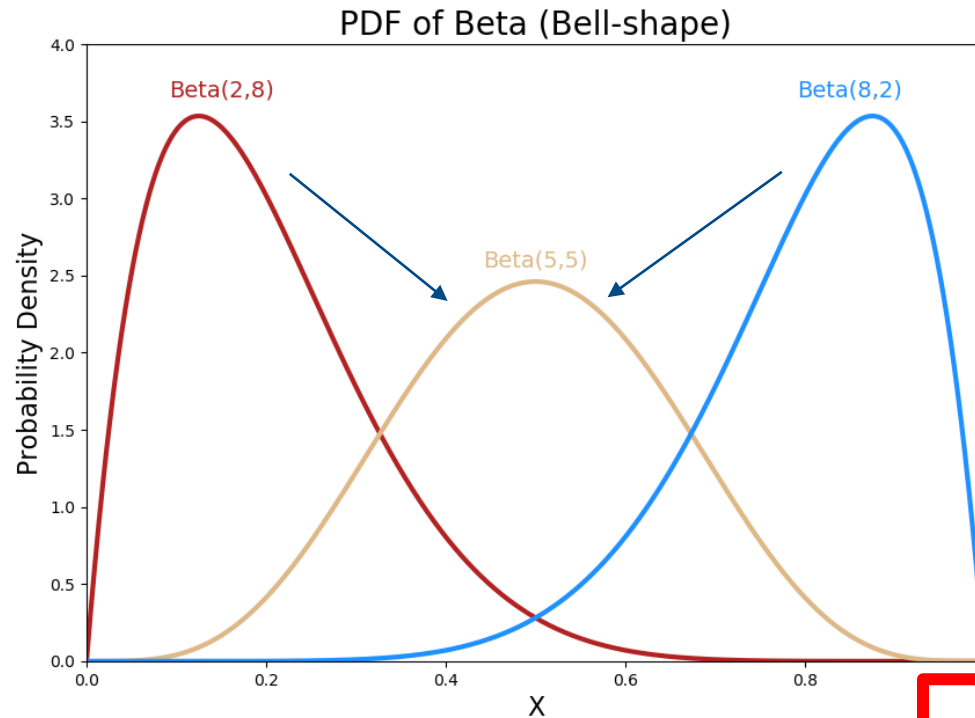
# Bagging/Random Forest Summary

- Bootstrap aggregation
  - Sampling from data
  - Sampling the variables (RF)
- Note for categorical variable:
  - Some packages can only handle numerical data (one hot-encoding)
  - Example: imagine your data has two types of houses, single family and other.
    - turn your categories into 0s and 1s (but what happens if you have 3 possible categories?).
    - Create a new column for each variable value and assign a 0 or 1
    - Create a new column for each variable value -1 “base” value (like in a GLM)
      - But now, stochastic sampling on the variables is not going to work at variable level

	Linear Models	CART	Bagging
	GLM	Single Decision Tree	Random Forest
Interpretability	Green	Green	Orange
Likelihood of Overfitting	Grey	Red	Light Green
Sensativity to Collinearity	Red	Light Green	Grey
Relative Predictive Power Given Strong Signal	Green	Grey	Light Green
Relative Predictive Power Given Weak Signal	Grey	Grey	Green
Relative Predictive Power Given Complex Variable Behaviors (Interactions + Mixtures + Non-linear Effects)	Red	Grey	Green
Skill Required	Red	Green	Orange
Speed of Development	Red	Green	Light Green

# Boosting (GBT/GBM)

# Beyond CART: Overcoming the limitations of the Single Decision Tree



## GBT = Gradient Boosted Trees

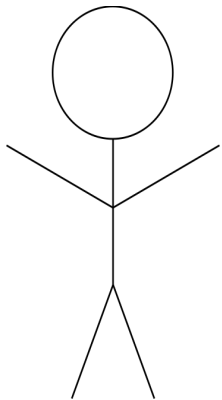
- Decision Trees: fine line between 'underfitting' and 'overfitting'
  - Random Forest are often 'underfitting'
- Solution: use the residuals of the first tree to reweight the data (greater weight given to higher residuals), this 'reweighted' data is used to create the next tree
  - Introduced by Jerome Friedman (1999)



# GBT = Gradient Boosted Trees

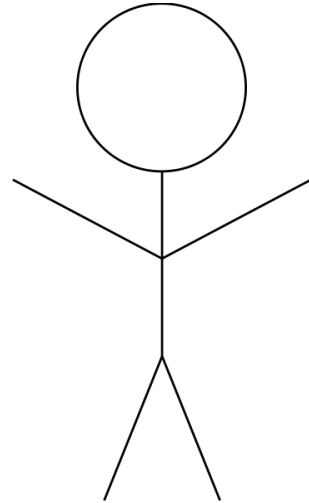
## Analogy

Sam is OK at guessing weights

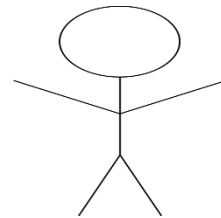


**Sam: 182**  
**Act: 180**

CKO notices Sam has a bias

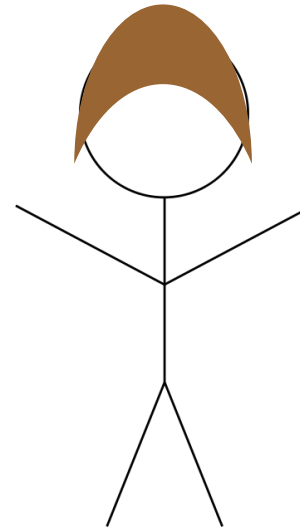


**Sam: 215**  
**Act: 200**

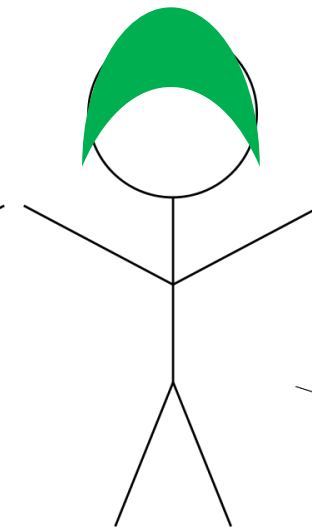


**Sam: 130**  
**Act: 145**

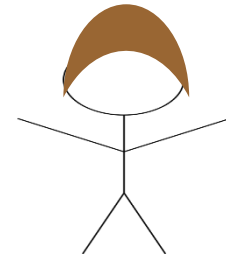
Jane notices I have a partial bias



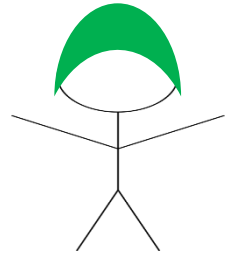
**CKO: 195**  
**Act: 200**



**CKO: 205**  
**Act: 200**



**CKO: 145**  
**Act: 145**



**CKO: 145**  
**Act: 145**

## GBT = Gradient Boosted Trees

- A function that controls ‘reweighting’ based on residuals
- Prevents ‘overcompensation’

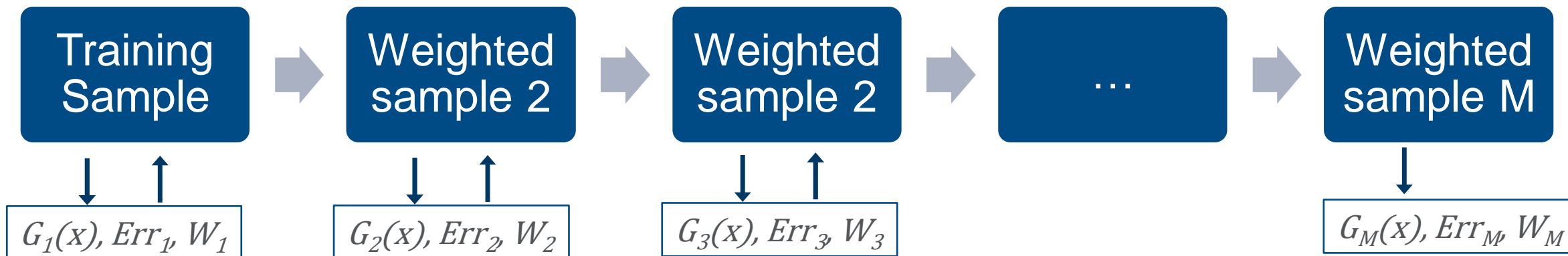






# Boosting

The original boosting algorithm: AdaBoost (Freund and Schapire 1997)



$$G(x) = \sum_{m=1}^M \alpha_m G_m(x)$$

$$\overline{Err} = \frac{1}{N} \sum_{n=1}^N I(y_i \neq G(x_i))$$

## Boosting in Practice: Hyperparameters

- Minimum Terminal Node Size
- Maximum Depth
- The number of splits per node
  - Controls the complexity of the boosted ensemble
  - Often very small numbers are used ( $d = 2, 3$ , etc.)
- The number of trees
  - Boosting can overfit if too many trees are used, although this overfitting tends to occur slowly if at all.
- Stochastic sampling rates (column & rows)  $\sim 0.6 \pm .2$
- The Learning Rate
  - How quickly trees zero in on Strong signal
- The Learning Rate Shrinkage parameter
  - It is used to avoid early overfitting
  - Typical values are 0.01 or 0.001, and the right choice can depend on the problem.
  - A very small shrinkage parameter results in needing a very large number of trees to achieve good performance
- Hyperparameter Search: Cross Fold Validation



# Gradient Boosted Trees

- Pros, Cons, & Limitations

	Linear Models	CART	Bagging	Boosting	
				Adjust Data	Raw Data
	GLM	Single Decision Tree	Random Forest	XGBoost, LightGBM, CATBoost	Base Python, R, H2O, ADABOOST
Interpretability	Green	Green	Orange	Orange	Grey
Likelihood of Overfitting	Grey	Red	Light Green	Orange	Orange
Sensativity to Collinearity	Red	Light Green	Grey	Grey	Grey
Relative Predictive Power Given Strong Signal	Green	Grey	Light Green	Green	Green
Relative Predictive Power Given Weak Signal	Grey	Grey	Green	Green	Green
Relative Predictive Power Given Complex Variable Behaviors (Interactions + Mixtures + Non-linear Effects)	Red	Grey	Green	Green	Green
Skill Required	Red	Green	Orange	Orange	Orange
Speed of Development	Red	Green	Light Green	Light Green	Light Green

# Evaluation – Model Performance



# Machine Learning Tree Performance

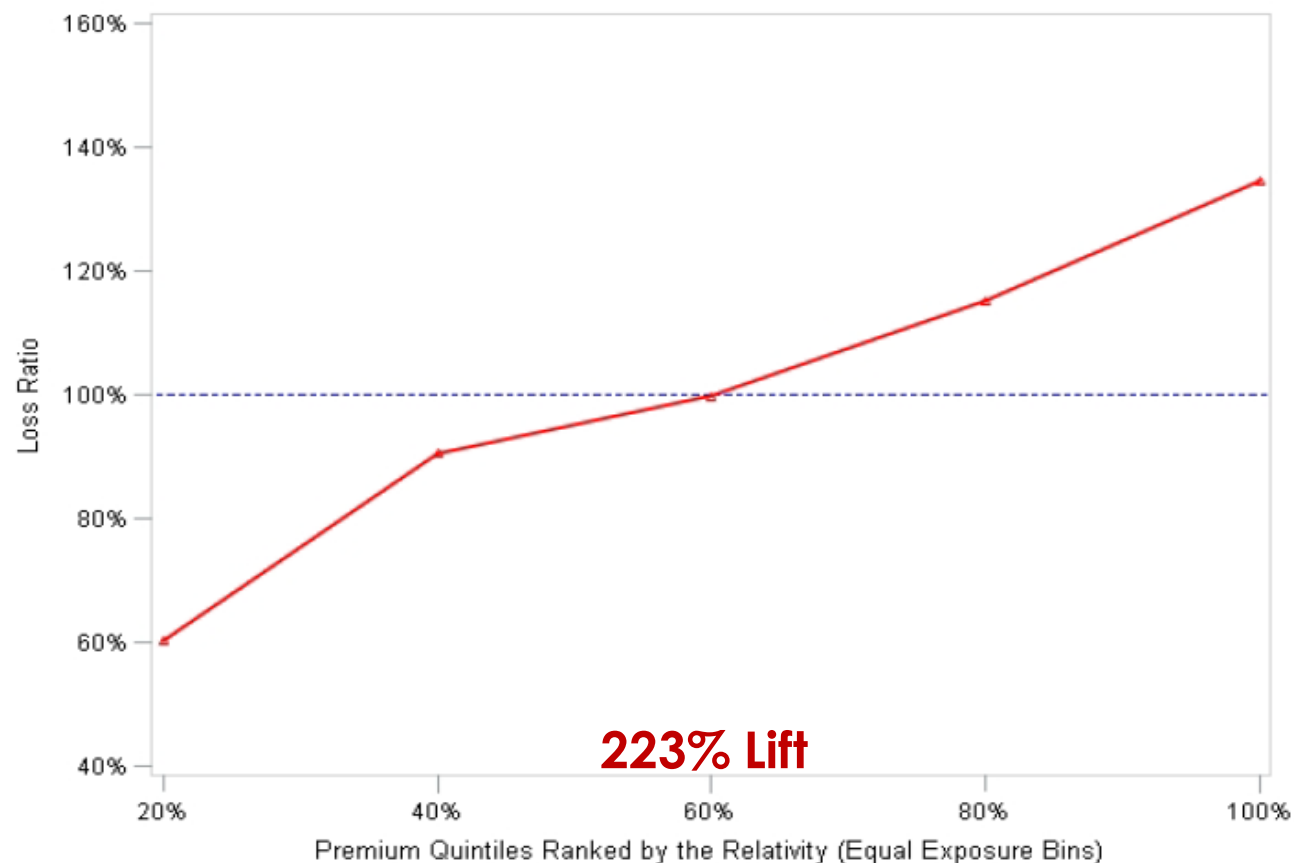
- **Predictive Accuracy**
  - Same metrics for GLM, RF, and GBT/GBM



# Machine Learning Tree Performance

- **Predictive Accuracy**
  - Same metrics for GLM, RF, and GBT/GBM
    - AUC, Gini, Lift

RACA GBT Symbols (on test data) – Random Holdout

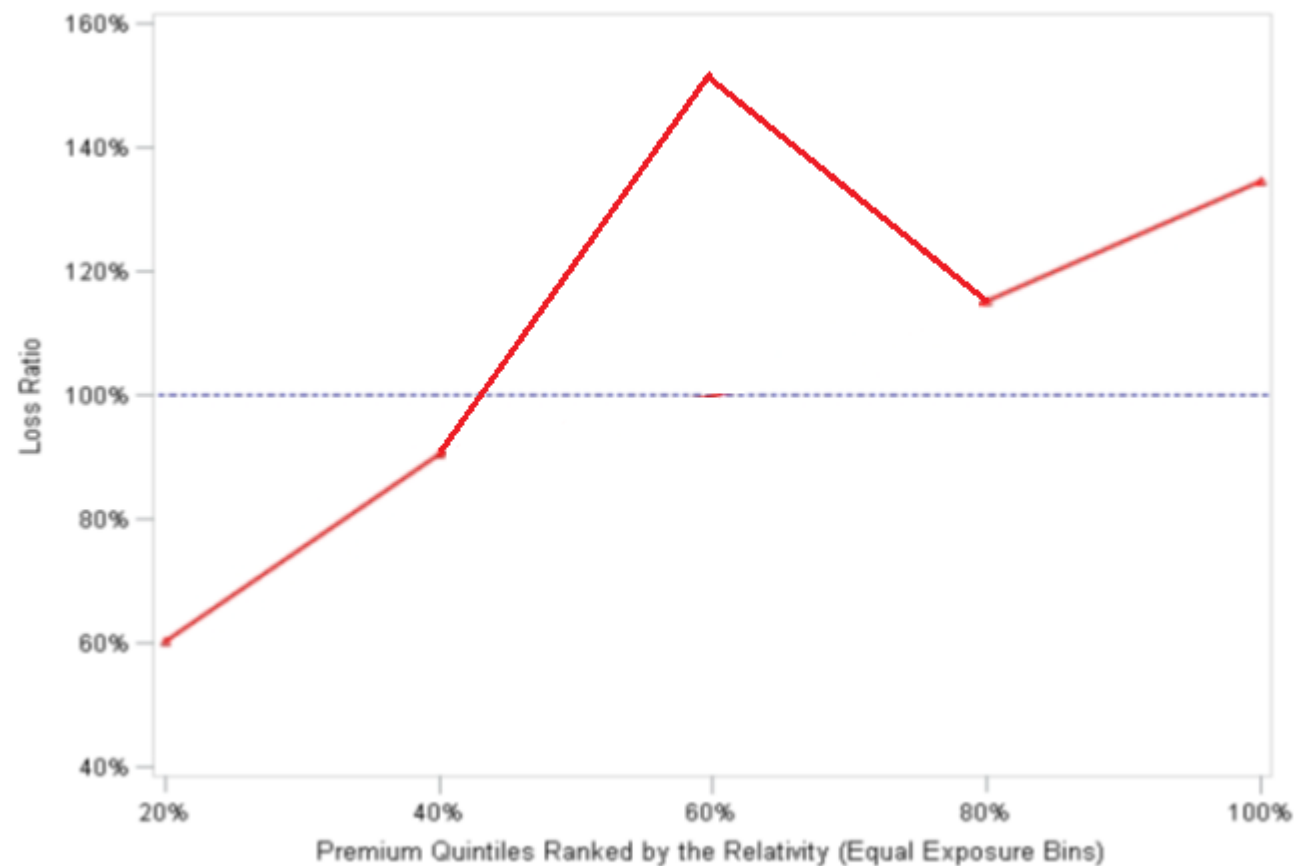




# Machine Learning Tree Performance

- **Predictive Accuracy**
  - Same metrics for GLM, RF, and GBT/GBM
    - AUC, Gini, Lift (No Reversals)

Simulated Bad Lift Chart

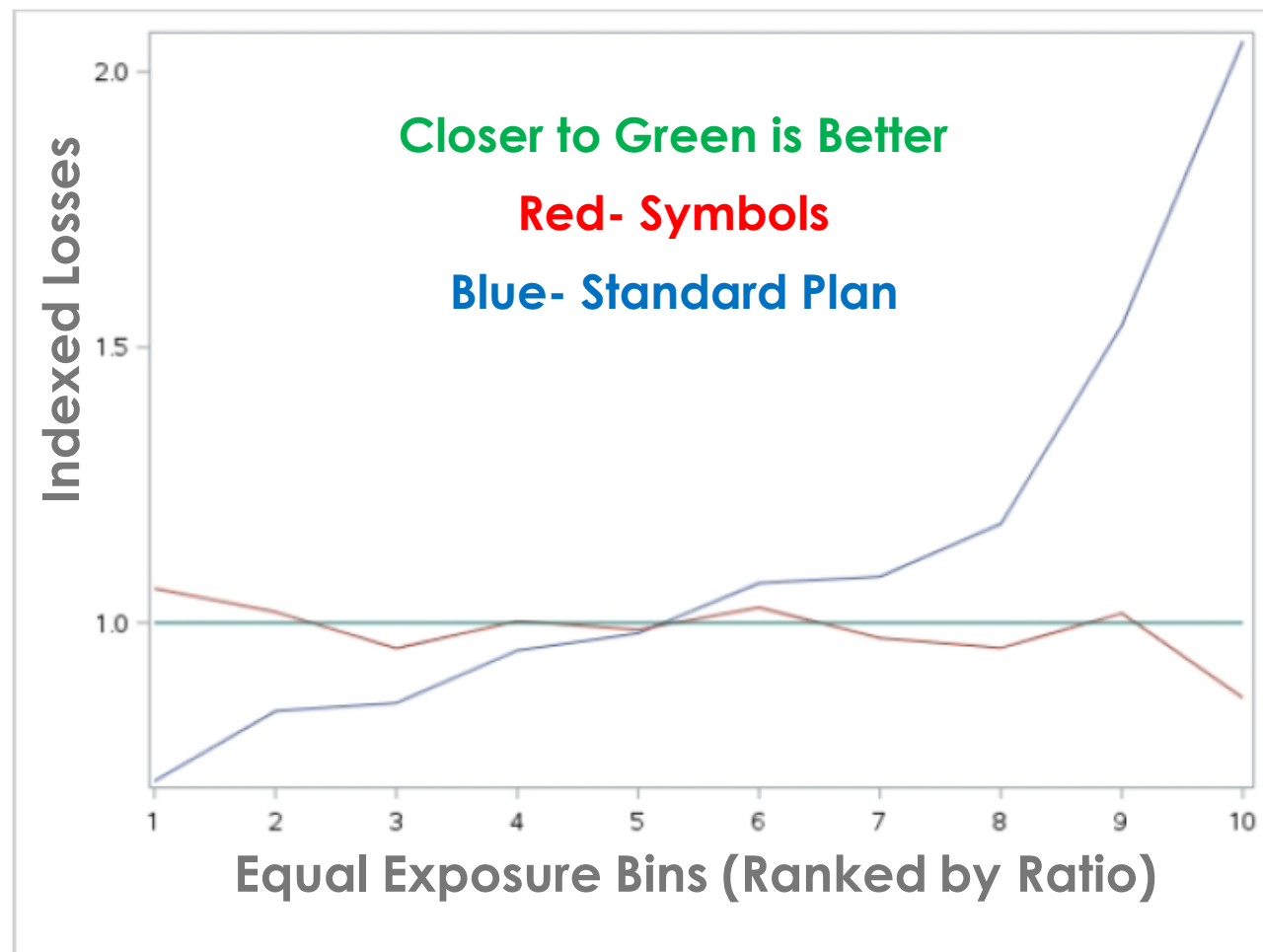




# Machine Learning Tree Performance

- **Predictive Accuracy**
  - Same metrics for GLM, RF, and GBT/GBM
    - AUC, Gini, Lift (No Reversals), Head-to-Head

RACA GBT Symbols vs Standard Plan (on test data)



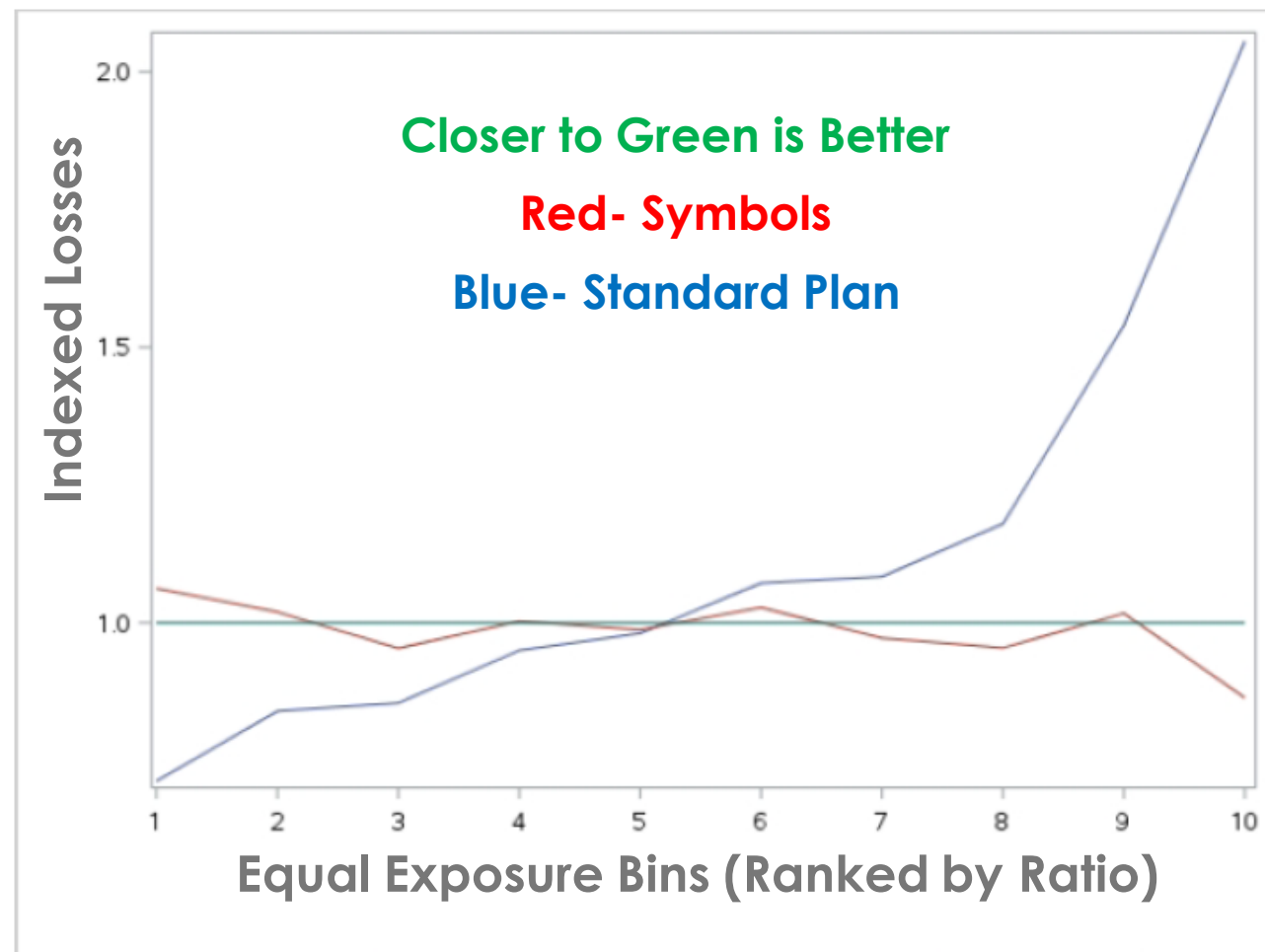


# Machine Learning Tree Performance

- **Predictive Accuracy**
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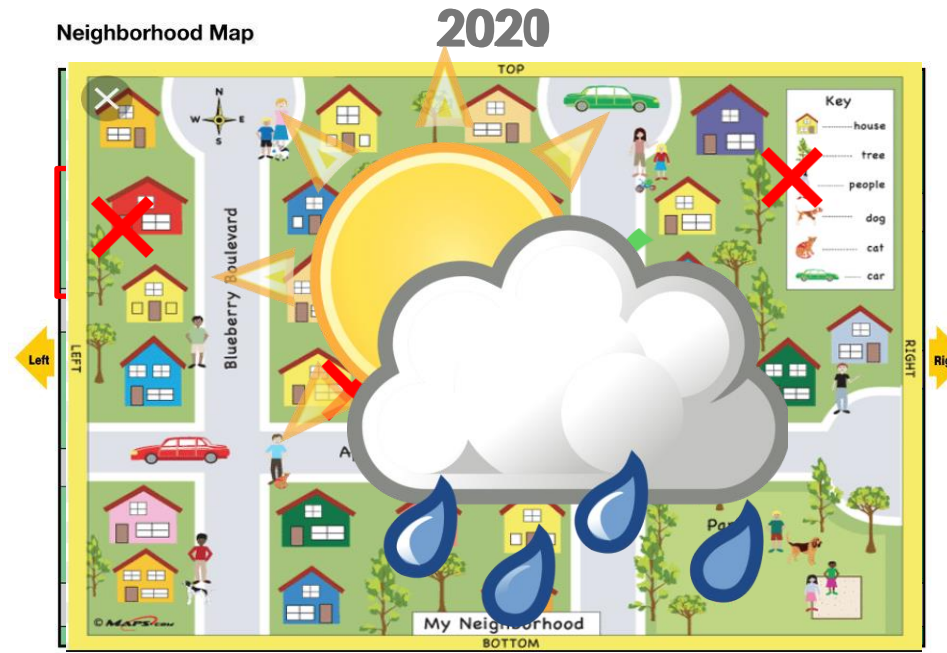
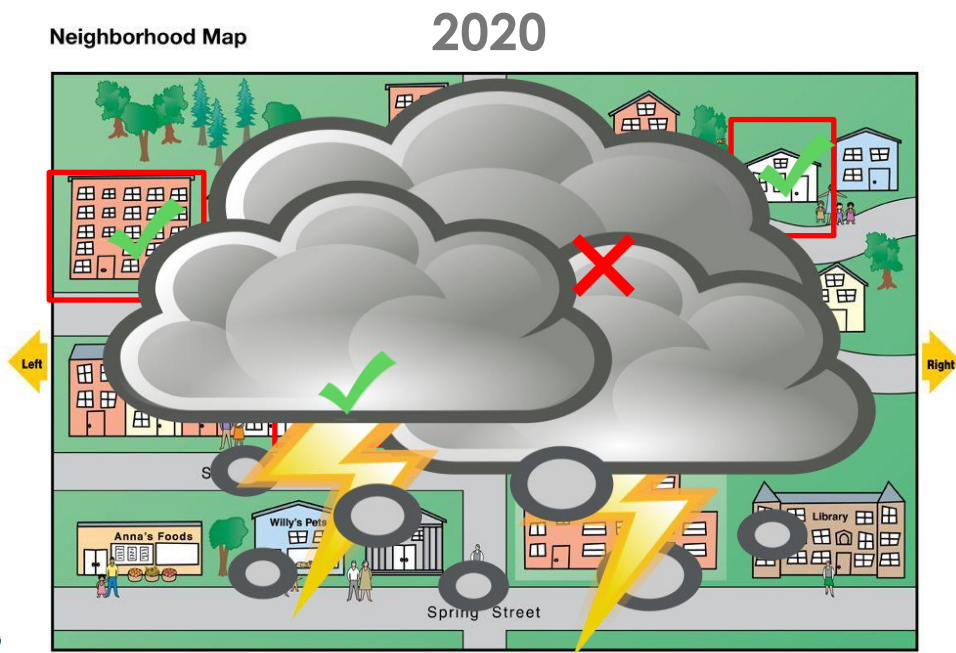
	Current	GBT Symbols	Improvement
<b>Lift</b>	NA	223%	223%
<b>Gini</b>	30.343	33.404	10%
<b>MSE</b>	2.594	0.398	652%
<b>MSE Weighted</b>	0.201	0.036	552%

GBT Symbols vs Standard Plan (on test data)



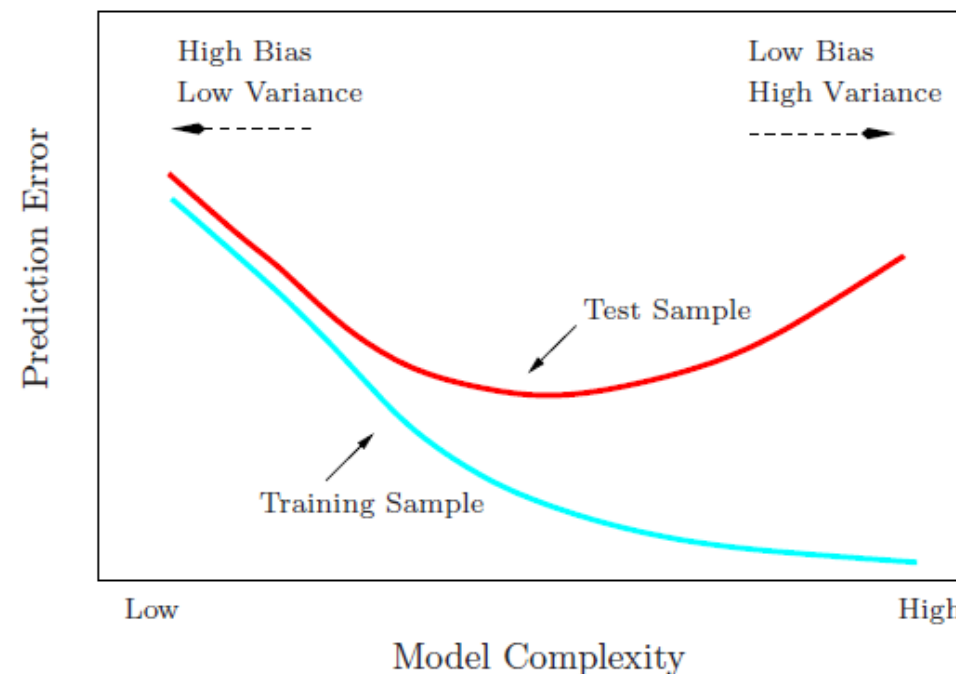
# Machine Learning Tree Performance

- **Predictive Accuracy**
  - Same metrics for GLM, RF, and GBT/GBM
    - AUC, Gini, Lift (No Reversals), Head-to-Head
  - Trees can overfit, need “True Test” data
    - Out of Time (train on 2014-2018, test on 2019-2020)
    - Out of Geography



# Machine Learning Tree Performance

- **Predictive Accuracy**
  - Same metrics for GLM, RF, and GBT/GBM
    - AUC, Gini, Lift (No Reversals), Head-to-Head
  - Trees can overfit, need “True Test” data
    - Out of Time (train on 2014-2018, test on 2019-2020)
    - Out of Geography
    - Multiple Random Samplings (different seeds)
  - Test set should be no more than 30% of total data
    - Hyperparameters are optimized based on data set size
  - Train vs Test Error



# When to use Trees



# When to use Trees

- Classification & Regression on Structured Data
  - Claims
  - Underwriting
  - Rating
- Real, but Hard to find Signal
  - Variable Interactions, Mixtures
  - Especially well suited for Low Frequency, High Severity Lines (Liability, Fire, etc.)
- Data
  - **Big** [enough] Data
    - Trees can overfit, be biased towards training data
    - Need enough data to reach credibility
  - Not **overly** concerned about Protected Classes
    - Data is orthogonal to Protected Classes
    - Underlying data has been transformed to remove bias
    - Risk of reengineering removed features

# Evaluation - Regulation



# Machine Learning Tree Quality

- **Predictive Accuracy**
- **Protecting the Consumer**
  - Control data that goes into model
  - Interpretability
    - Do you understand “the story”?
      - Could a failure to understand “the story” cause an undesirable outcome?

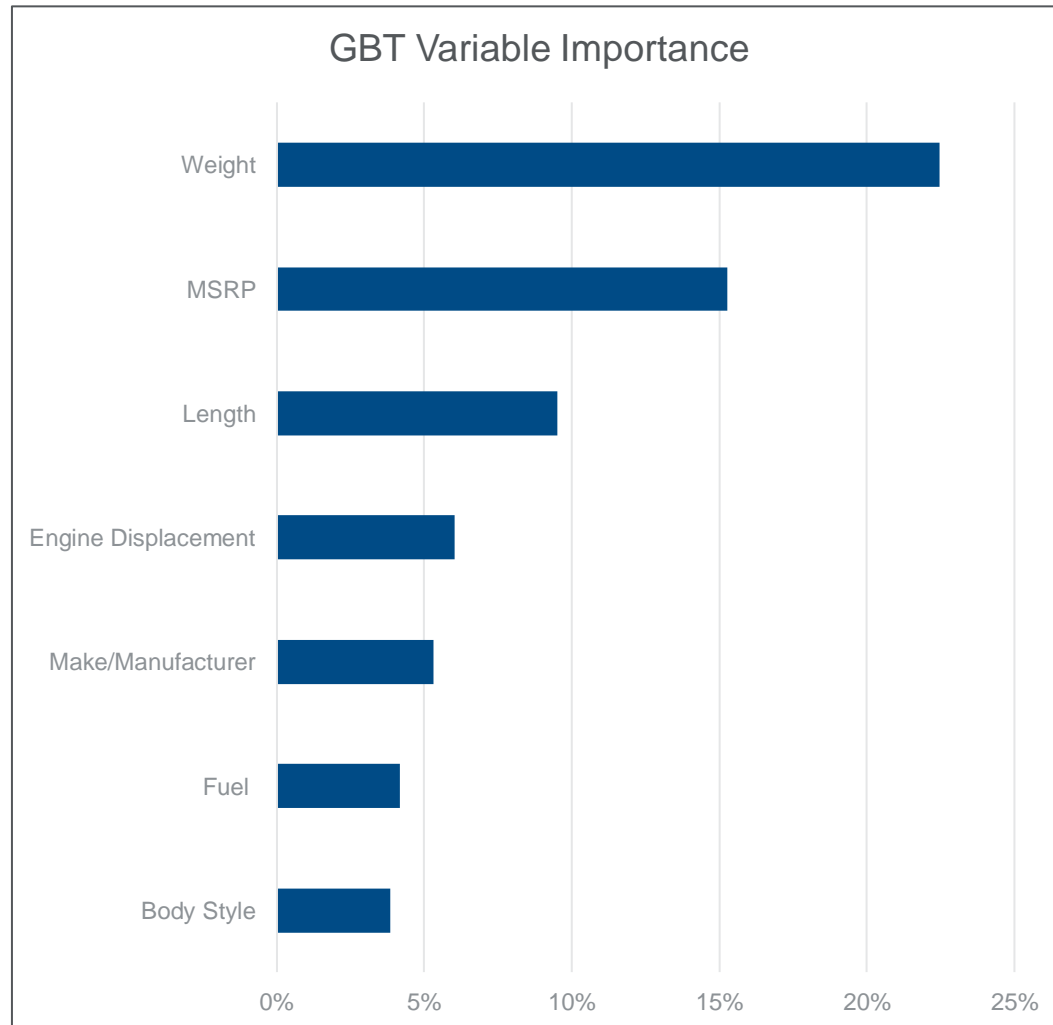


# Machine Learning Tree Quality

- **Predictive Accuracy**
- **Protecting the Consumer**
  - Control data that goes into model
  - Interpretability
    - Do you understand “the story”?
      - Could a failure to understand “the story” cause an undesirable outcome?
    - Variable Importance: Weighted measure of how many records are affected by each Variable throughout entire Model



# Variable Importance



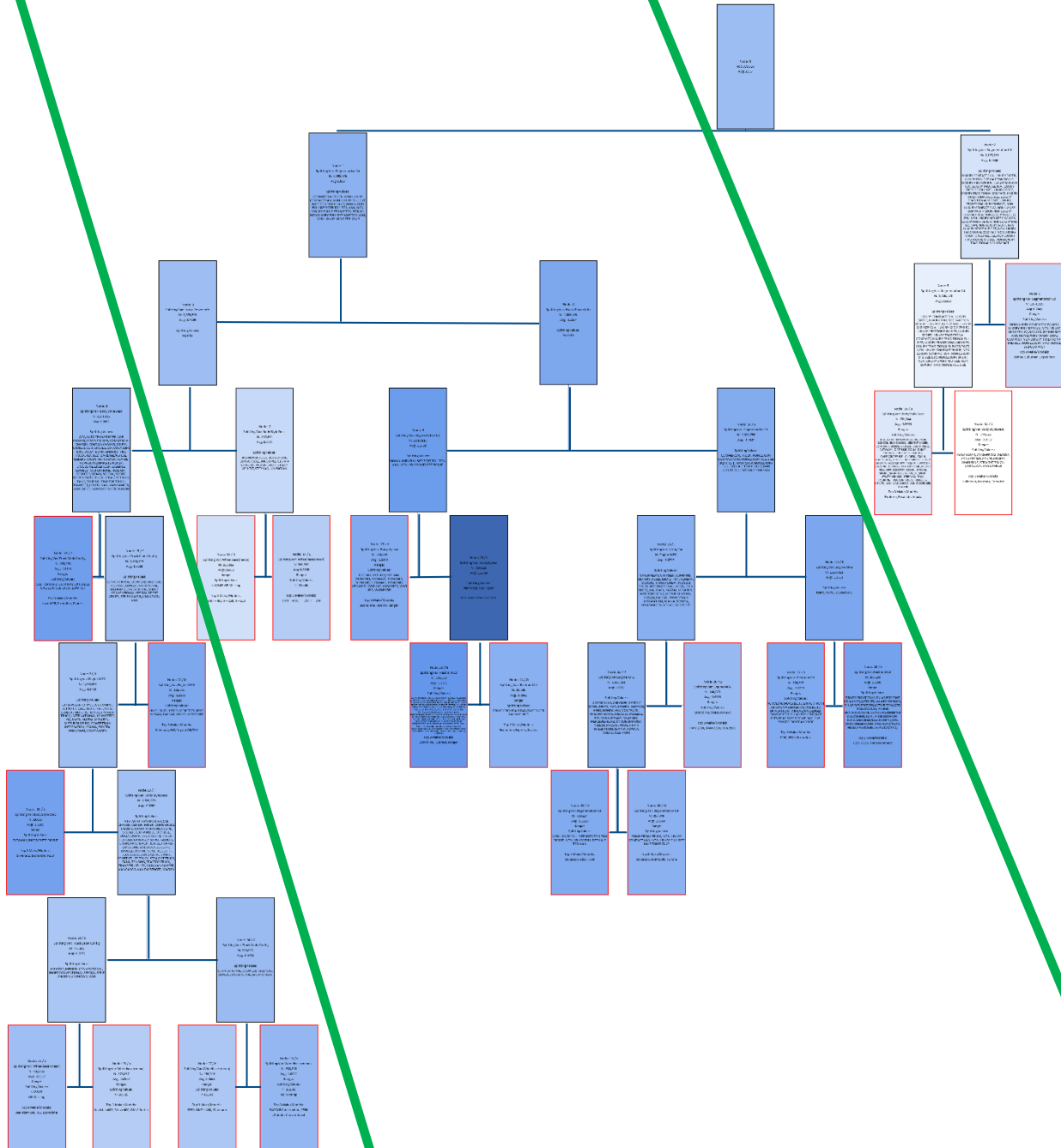


# Machine Learning Tree Quality

- **Predictive Accuracy**
- **Protecting the Consumer**
  - Control data that goes into model
  - Interpretability
    - Do you understand “the story”?
      - Could a failure to understand “the story” cause an undesirable outcome?
    - Variable Importance: Weighted measure of how many records are affected by each Variable throughout entire GBT
    - Interpretative trees (Surrogate model)
      - Fit a simple Decision Tree to the GBT model predictions – AKA Data Mine the GBT Predictions
      - Easy to interpret – tells a story



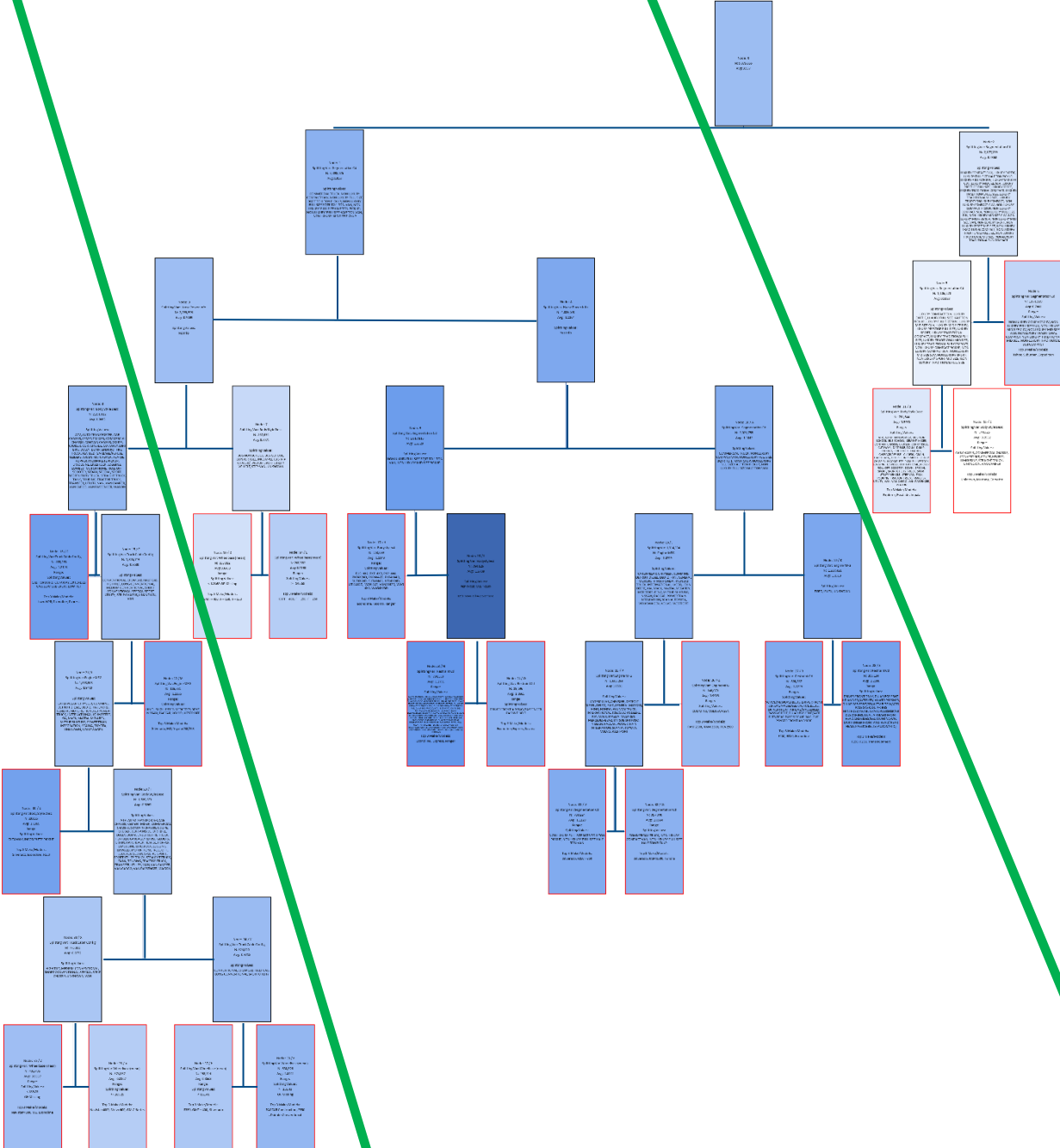
# Interpretive Trees





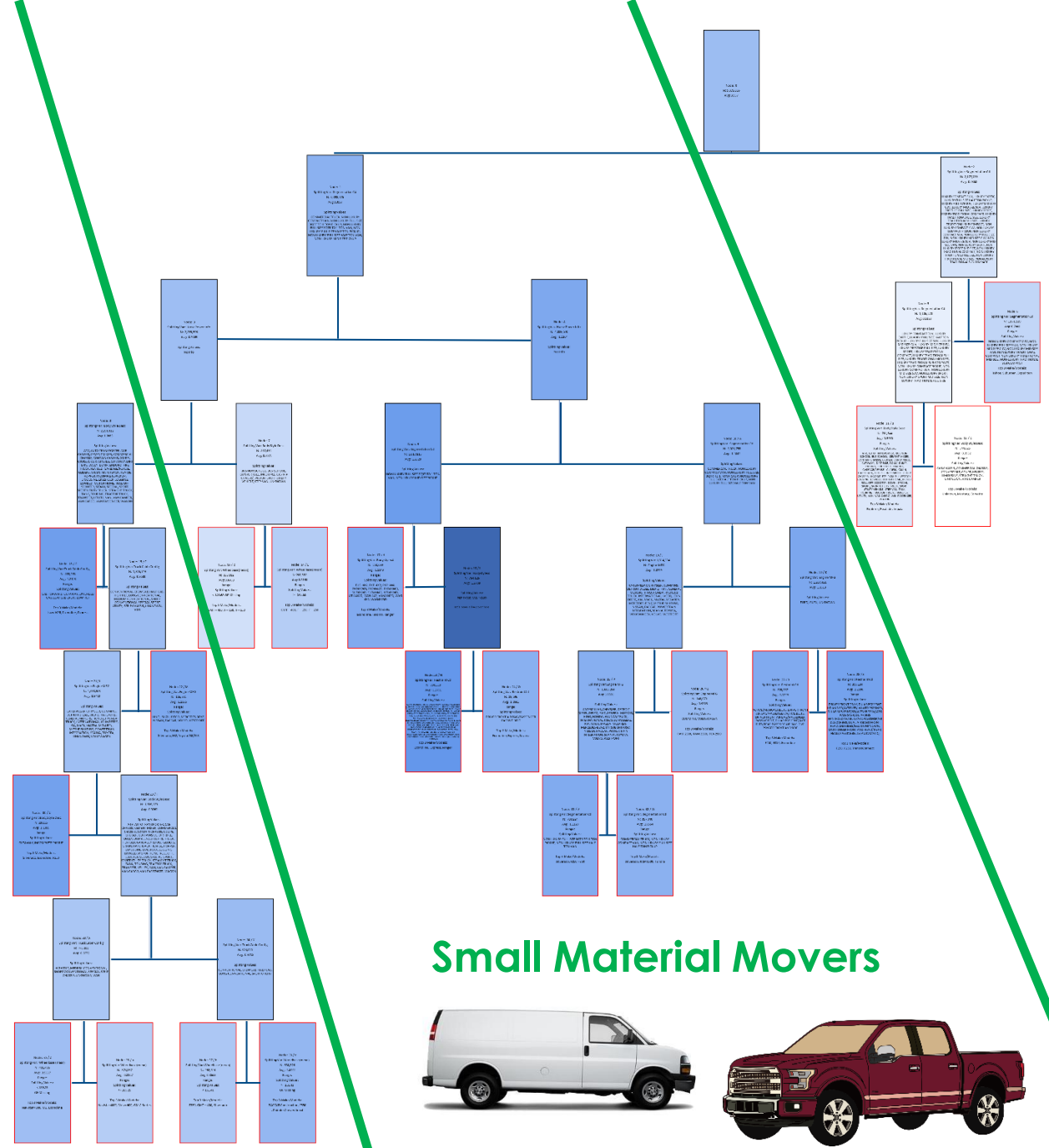
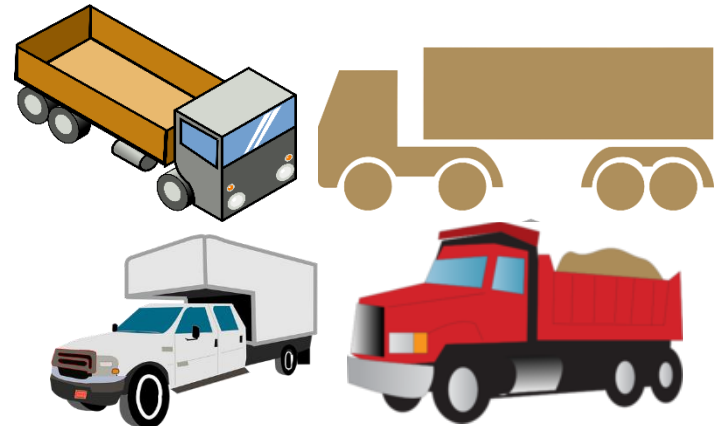
# Interpretive Trees

## Material Movers



# Interpretive Trees

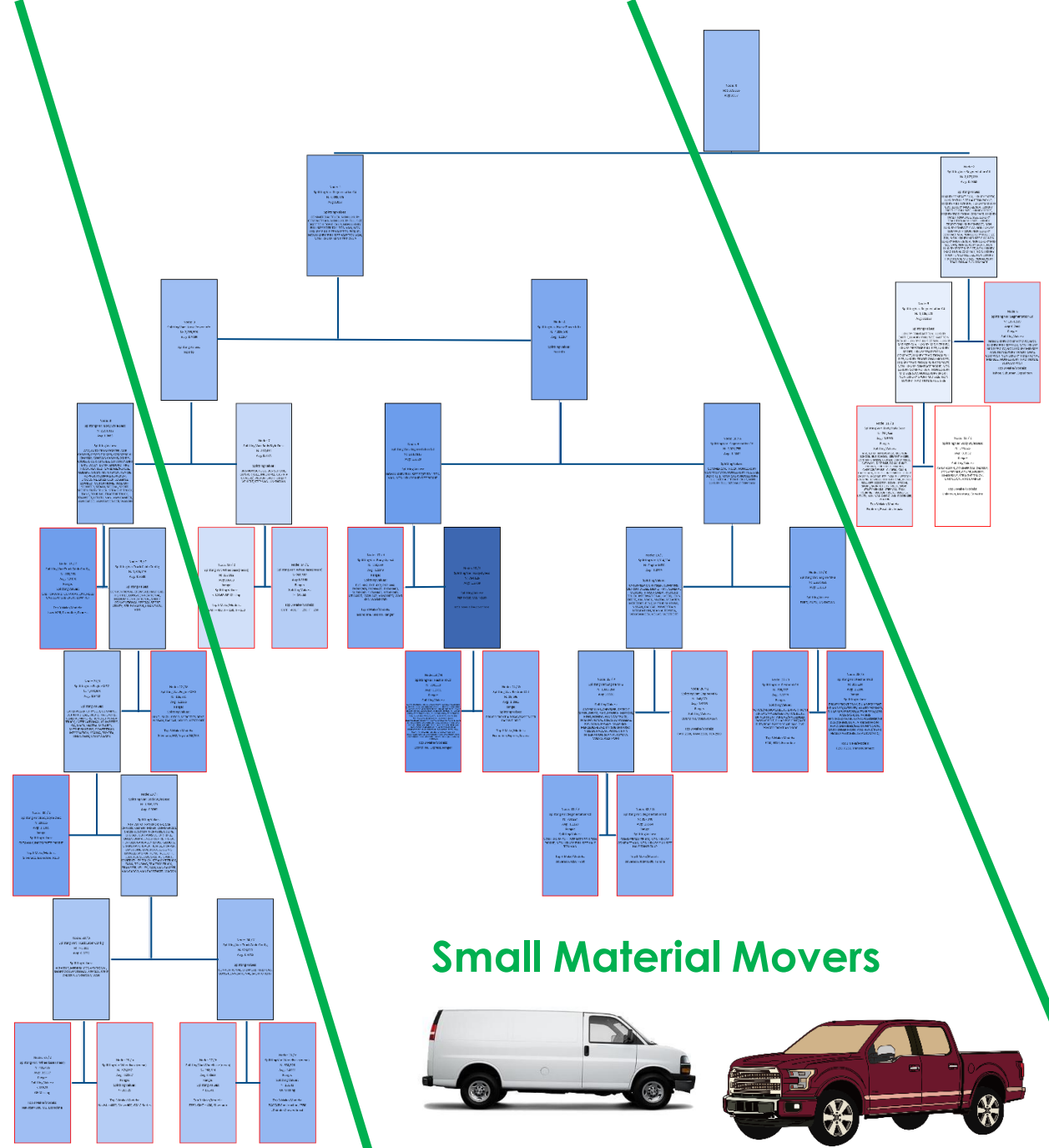
## Material Movers



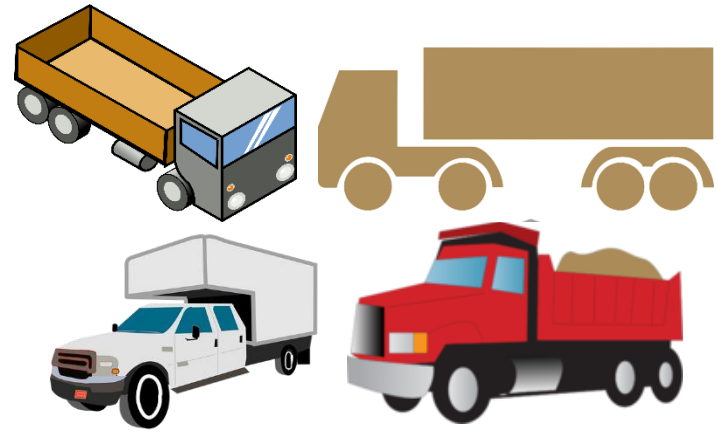
## Small Material Movers



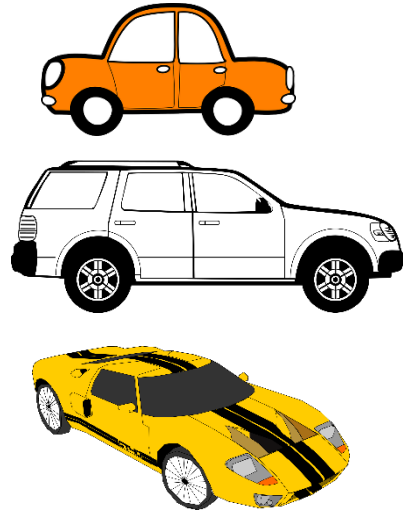
# Interpretive Trees



## Material Movers



## People Movers



## Small Material Movers





# Machine Learning Tree Quality

- **Predictive Accuracy**
- **Protecting the Consumer**
  - Control data that goes into model
  - Interpretability
    - Do you understand “the story”?
      - Could a failure to understand “the story” cause an undesirable outcome?
    - Variable Importance: Weighted measure of how many records are affected by each Variable throughout entire GBT
    - Interpretative trees (Surrogate model)
      - Fit a simple Decision Tree to the GBT model predictions – AKA Data Mine the GBT Predictions
      - Easy to interpret – tells a story
    - Individual Conditional Expectation (ICE)
      - Show Correlation between Variable’s Value and GBT Prediction
      - Hard to interpret
    - Partial Dependence Plots
      - Requires rerunning of the model while iteratively setting each variable to a constant level
        - Long process, only takes a ~‘univariate’ approach and leaves out 2+ way interactions
      - Hard to interpret
    - Shap Index
      - Really great for understanding ‘univariate’ approach
      - Not useful for 2+ way interactions & Mixtures



# Machine Learning Tree Quality

- Things to look for
  - Can the Actuaries/Data Scientists tell a story that makes sense?
  - Hyperparameter Search
    - Good: Exhaustive/Factorial (Requires multiple rounds), Bayesian, Random
    - Bad: No optimization (even on Random Forest)
  - Truly “Random” Test Data
    - Weather Damage should always be tested using Out of Time/Out of Geography methods
  - “The Smell Test”
    - E.g., predictors=“engine size & driver age” or “# of windows per capita”
      - Partial (or preferably Repair\*) questionable variables
        - Without ‘Repairing’ data, our understanding is that Trees can find signal related to undesirable predictor variables
      - Intuitive explanations for all important variables

\* Feldman et al 2015: certifying & removing disparate impact





## Machine Learning Tree Quality

- Common Insurance Data Science Mistakes
  - Non-sensical variables
  - Overfitting
  - Non-random test data (out of time/geography is key)
  - Minimum terminal node size is too small
    - For low frequency/high severity lines, recommend minimum size >5,000 records (could be 50,000)
      - Analogy to GLM Credibility Standards
  - Trees are too deep
    - Depth of 50 =  $2^{50}$  = 1 billion terminal nodes → overfitting
    - Recommended maximum depth : RF  $\leq 30$  , GBT  $\leq 13$
  - Not removing collinear predictors + one-hot encoding trap
    - Can negate stochastic column sampling in GBT & RF
  - Non-coherent predictions
    - Rates shouldn't double when you turn 25 only to go back down when your 26
- Some divergence from standard operating procedures is not necessarily “wrong”, maybe just suboptimal



# Summary

## Trees are

- Not “AI”
- Well Established
- Faster & Easier than GLMs
- Very Accurate
- More interpretable than people realize

**Thank you**